

Exoplanetary Atmospheres

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Jonathan Fortney (UCSC)

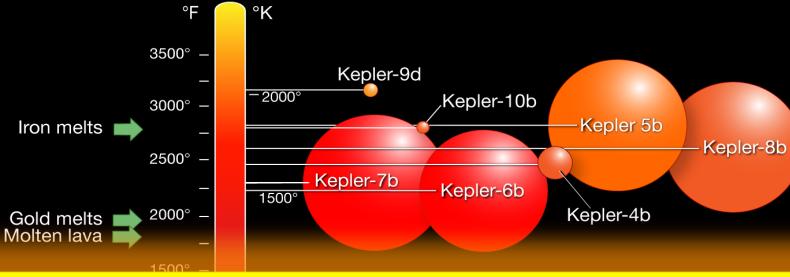
Travis Barman (Lowell Obs.)

*July 19, 2013. Heidelberg Convention Center
Protostars & Planets VI, Heidelberg, Germany*

Image Credits: ESA – C. Carreau

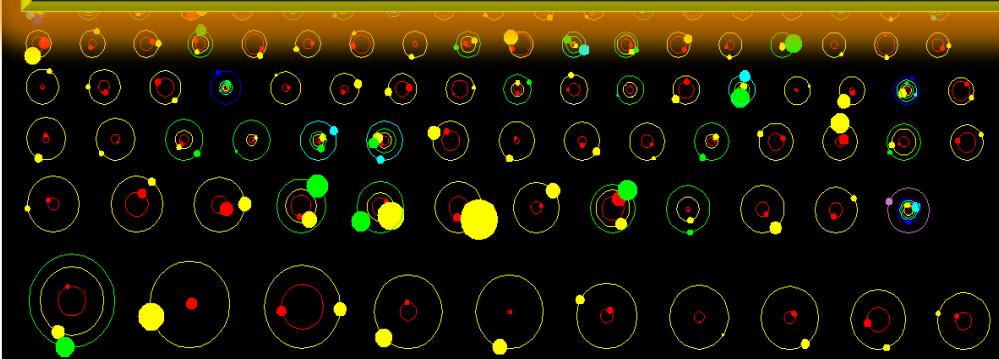
Exoplanets are extremely diverse in their physical characteristics

Exoplanet Temperatures and Sizes



Question at the new frontier:

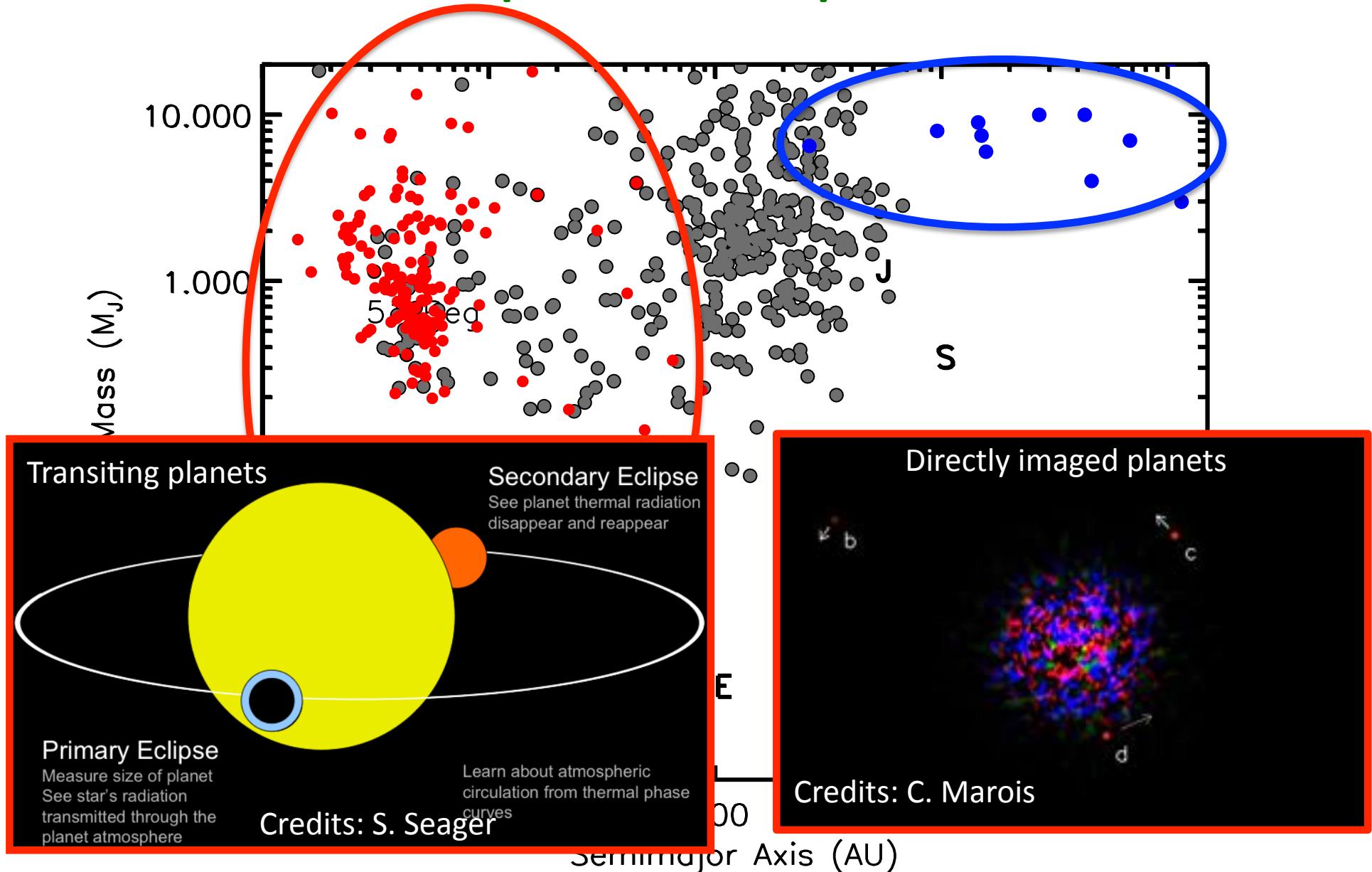
How diverse are the chemical compositions
and physical processes in exoplanets?



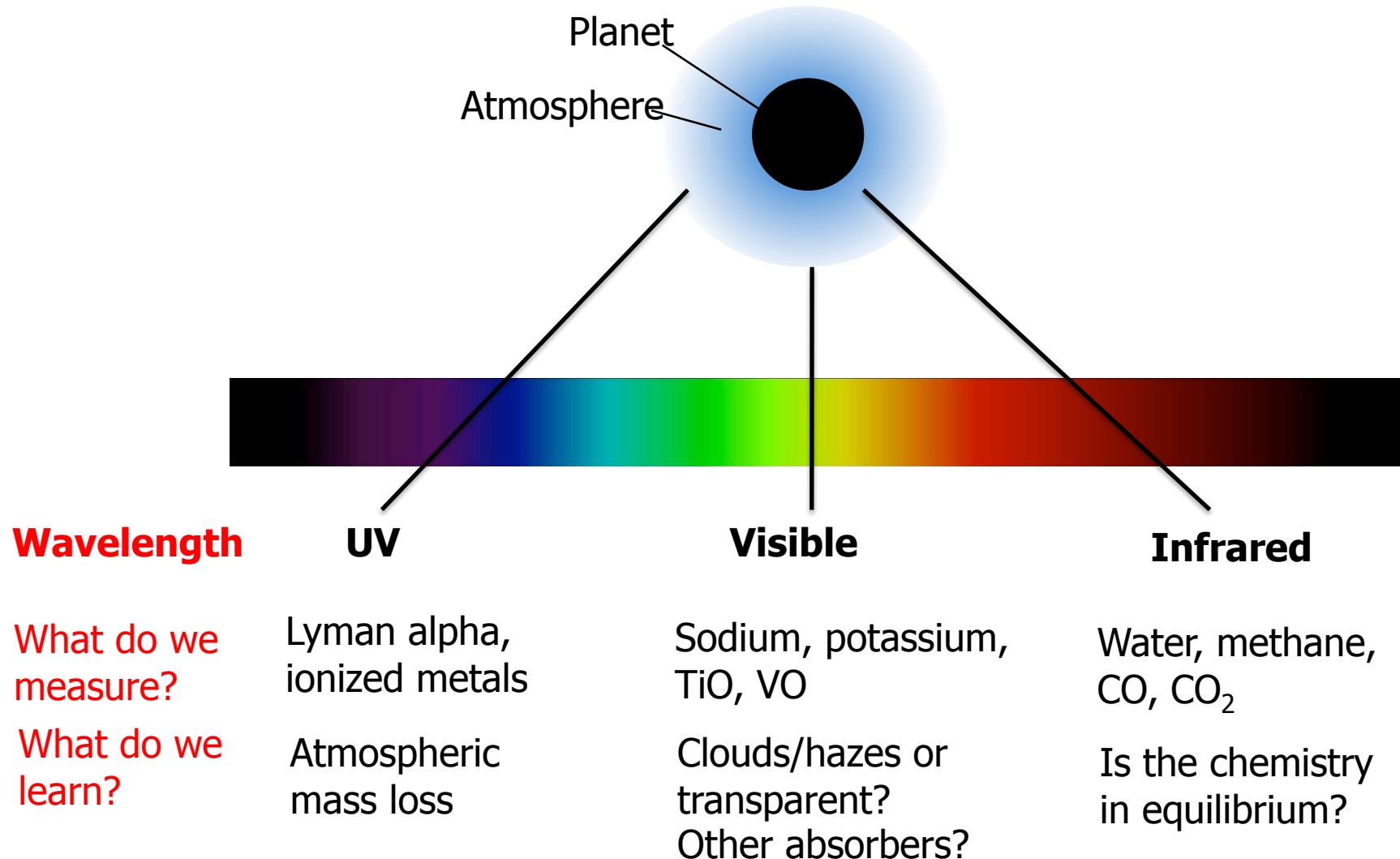
Hot Jupiter! Super-Earth!

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Exoplanet Population



What Do We Learn From Transmission Spectroscopy?



Outline

- ✧ Theory of Exoplanetary Atmospheres
- ✧ Atmospheres of Hot Jupiters
- ✧ Atmospheres of Directly-imaged Planets
- ✧ Atmospheres of Hot Neptunes
- ✧ Atmospheres of Super-Earths
- ✧ Frontier Problems and Future Outlook

Models of Exoplanetary Atmospheres

1-D Equilibrium models of exoplanetary atmospheres

$$\frac{dP}{dr} = -\rho g$$

$$\frac{dI_\lambda}{d\tau_\lambda} = -(1 + \frac{\sigma_\lambda}{\kappa_\lambda})I_\lambda + \frac{j_\lambda}{\kappa_\lambda}$$

$$\int_0^\infty \kappa_\lambda [J_\lambda - B_\lambda] d\lambda = 0$$

$$\frac{dT}{dr} = -\frac{\gamma - 1}{\gamma} \frac{\mu g}{k_B}$$

$$P = \frac{\rho k_B T}{\mu}$$

Model Parameters

- Day-night redistribution: P_n, P_1, P_2
- Extra absorber: $P_{abs}, (\lambda_0, \lambda_1), \kappa_e$
- Composition (f_z) + clouds, etc.

Boundary Conditions

- Stellar Irradiation (Kurucz Model)
- Intrinsic Energy source

Chemical Equilibrium

$$\frac{G(T)}{RT} = \sum_{i=1}^m \left\{ n_{\phi i} \left[\frac{\Delta G_{\phi i}(T)}{RT} + \ln P + \ln \left(\frac{n_{\phi i}}{N} \right) \right] \right\}_{\phi=1}$$
$$+ \frac{1}{RT} \sum_{\phi=2}^{s+1} [n_{\phi i} \Delta G_{\phi i}(T)]_{i-1}$$

$$\sum_{i=1}^m [v_{\phi ij} n_{\phi i}]_{\phi=1} + \sum_{\phi=2}^{s+1} [v_{\phi ij} n_{\phi i}]_{i-1} = b_j \quad \text{for } j = 1 \rightarrow k$$

$$B_{CO} = A_C + A_O + \frac{P_{H_2}^2}{2K_1(T)} - \sqrt{\left[A_C + A_O + \frac{P_{H_2}^2}{2K_1(T)} \right]^2 - 4A_C A_O}$$

Caveats

- Parameters
- Chemical equilibrium and compositions
- Computation time
- Artificial sources and sinks

Marley et al. 1996; Seager & Sasselov 1998; Allard et al. 2001; Sudarsky et al. 2003;
Seager et al. 2005; Barman et al. 2005; Fortney et al. 2006; Burrows et al. 2007

Models of Exoplanetary Atmospheres

1-D parametric models of exoplanet atmospheres

$$\frac{dP}{dr} = -\rho g$$

$$\frac{dI_\lambda}{d\tau_\lambda} = -(1 + \frac{\sigma_\lambda}{\kappa_\lambda})I_\lambda + \frac{j_\lambda}{\kappa_\lambda}$$

$$\left| \begin{array}{l} \int_0^\infty \kappa_\lambda [J_\lambda - B_\lambda] d\lambda = 0 \\ P = P(T) \\ \frac{dT}{dr} = -\frac{\gamma-1}{\gamma} \frac{\mu g}{k_B} \end{array} \right.$$

$$P = \frac{\rho k_B T}{\mu}$$

Model Parameters

- Day-night redistribution: P_n, P_1, P_2
- Extra absorber: $P_{abs}, (\lambda_0, \lambda_1), \kappa_e$
- Composition (f_z) + clouds, etc.

Boundary Conditions

- Stellar Irradiation (Kurucz Model)
- Intrinsic Energy source

Chemical Equilibrium

$$[X] = f_z \times [X]_{solar}$$

$$\frac{G(T)}{RT} = \sum_{i=1}^m \left\{ n_{\phi i} \left[\frac{\Delta G_{\phi i}(T)}{RT} + \ln P + \ln \left(\frac{n_{\phi i}}{N} \right) \right] \right\}_{\phi=1}^m$$

Perturbations to equilibrium or uniform mixing

$$\sum_{i=1}^m [v_{\phi i j} n_{\phi i}]_{\phi=1} + \sum_{\phi=2}^s [v_{\phi i j} n_{\phi i}]_{i=1} = b_j \quad \text{for } j = 1 \rightarrow k$$

$$B_{CO} = A_C + A_O + \frac{P_{H_2}^2}{2K_1(T)} - \sqrt{\left[A_C + A_O + \frac{P_{H_2}^2}{2K_1(T)} \right]^2 - 4A_C A_O}$$

Caveats

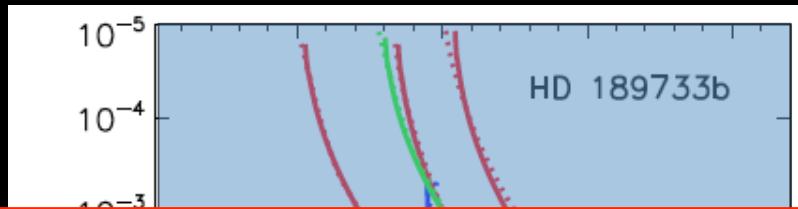
- Parameters
- Chemical equilibrium and compositions
- Computation time
- Artificial sources and sinks

Madhusudhan & Seager 2009; Miller-Ricci et al. 2009; Lee et al. 2012, Line et al. 2012; Benneke et al. 2012

Theory of Exoplanetary Atmospheres

- Equilibrium and non-Equilibrium chemistry (Burrows & Sharp 1999; Lodders & Fegley 2002; Moses et al. 2011)
- Temperature structures in irradiated atmospheres (Hansen et al. 2008; Spiegel et al. 2009; Guillot et al. 2010; Heng et al. 2011)
- Clouds, hazes, condensates (Helling et al. 2008; Lecavelier des Etangs 2008; Marley et al. 2013; Morley et al. 2013)
- Atmospheric dynamics (Cho et al. 2008; Showman et al. 2008,2009; Heng et al. 2011; Rauscher & Menou 2012)
- Exospheres and atmospheric escape (Vidal Madjar et al. 2003; Murray-Clay et al. 2009; Koskinen et al. 2012)
- Statistical retrieval codes (Madhusudhan & Seager 2009; Madhusudhan et al. 2011; Line et al. 2012; Lee et al. 2012; Benneke et al. 2012)
- Carbon-rich atmospheres (Madhusudhan et al. 2011; Madhusudhan 2012)
- Terrestrial-size exoplanets (Kaltenegger et al. 2011; Schaffer et al. 2011)
- High-Temperature opacity linelists (Rothman et al. 2005,2008; Freedman et al. 2008; Tennyson & Yurchenko 2012; ExoMol Project) – **Most important inputs!**

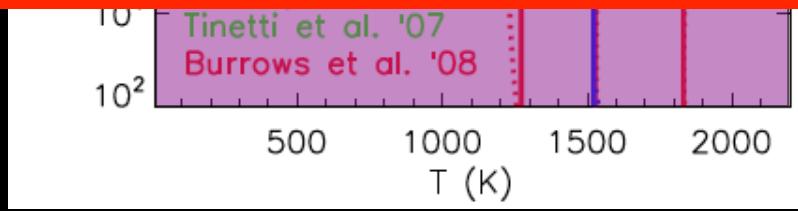
Temperature Structures in Highly Irradiated Atmospheres



Low optical depth limit

$$T(\tau) = T_{\text{eff}} \left[\frac{3\tau}{4} + \frac{1}{2} \right]^{1/4}$$

Measuring temperature structures allows us to constrain the thermal, chemical, and radiative processes in the observable atmosphere



Diffusion approximation
Large optical depth limit

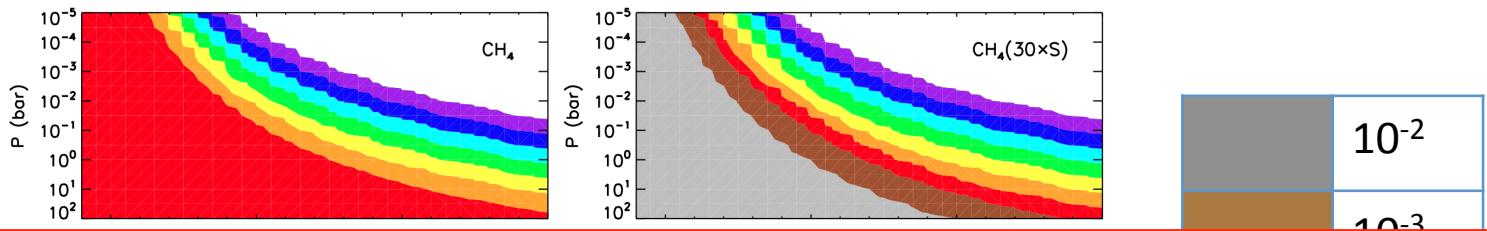
$$F = -\frac{16}{3} \frac{\sigma T^3}{\kappa \rho} \frac{dT}{dz} = \frac{16\sigma T^3}{3} \frac{dT}{d\tau}$$

Two stream gray model (Hansen, 2008; Guillot 2010; Heng et al. 2011)

$$T^4 = \frac{3}{4} T_{\text{eff}}^4 \left[\tau + \frac{2}{3} \right] + \mu_0 T_0^4 \left[1 + \frac{3}{2} \left(\frac{\mu_0}{\gamma} \right)^2 - \frac{3}{2} \left(\frac{\mu_0}{\gamma} \right)^3 \ln \left(1 + \frac{\gamma}{\mu_0} \right) - \frac{3}{4} \left(\frac{\mu_0}{\gamma} \right) e^{-\gamma\tau/\mu_0} \right]$$

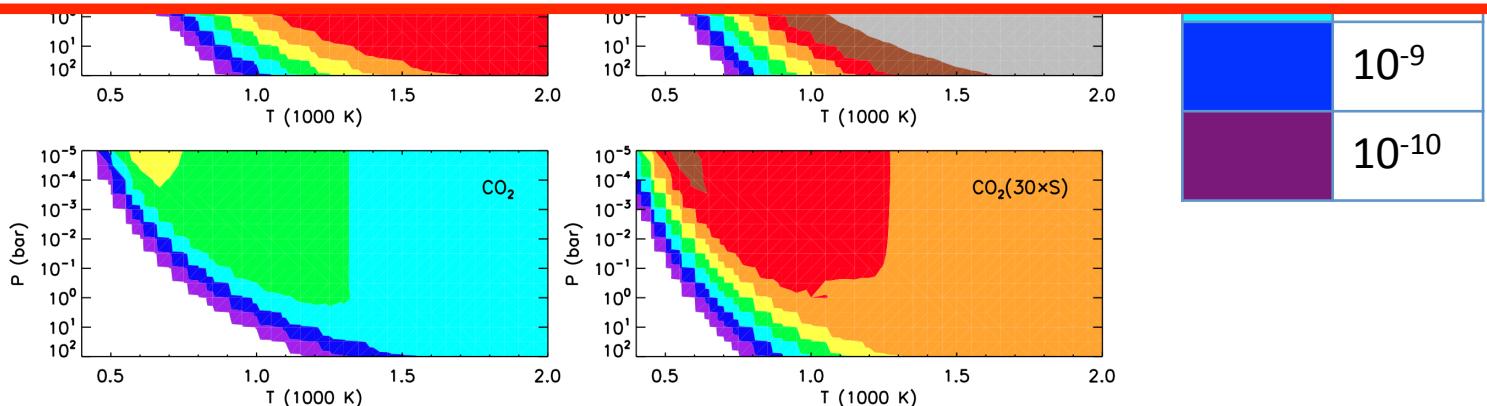
Chemistry in H₂-rich Atmospheres

(Molecular mixing ratios assuming chemical equilibrium)



For solar composition atmospheres:

1. H₂O should be dominant O carrier at all T
2. CO should be dominant C carrier at high T
3. CH₄ should be dominant C carrier at low T



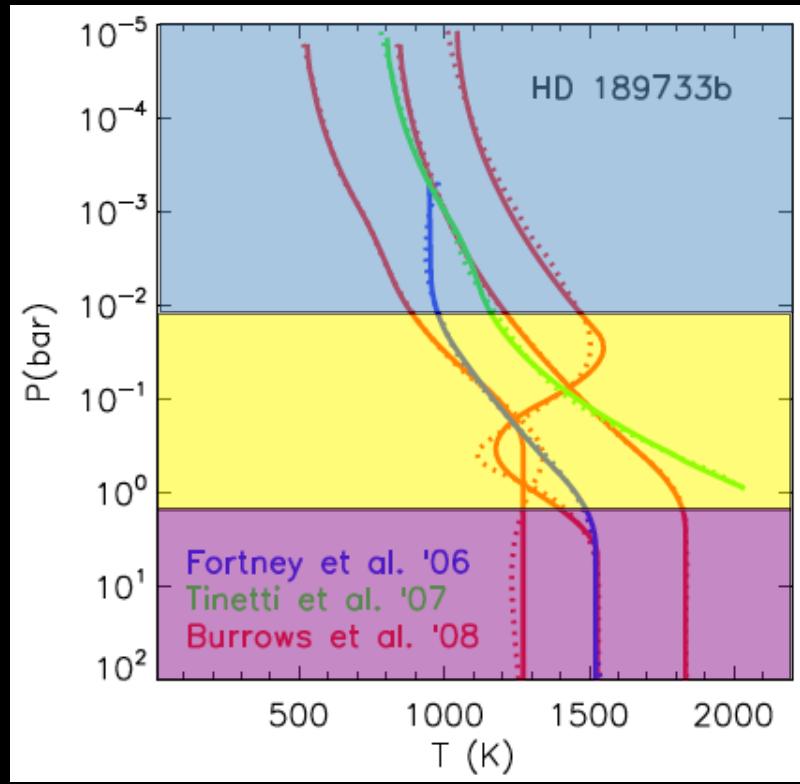
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Advances in hot Jupiter Atmospheres

- Temperature structures and thermal inversions
- Molecular and Atomic abundances
- Phase curves and atmospheric dynamics
- Hazes and clouds
- Two distinct observational advances
 - Ground-based spectroscopy
 - HST WFC3 spectroscopy
- Atmospheric detections of radial velocity planets
- Exospheres and atmospheric escape
- Inferences of Polarization

Temperature Structures in Highly Irradiated Atmospheres

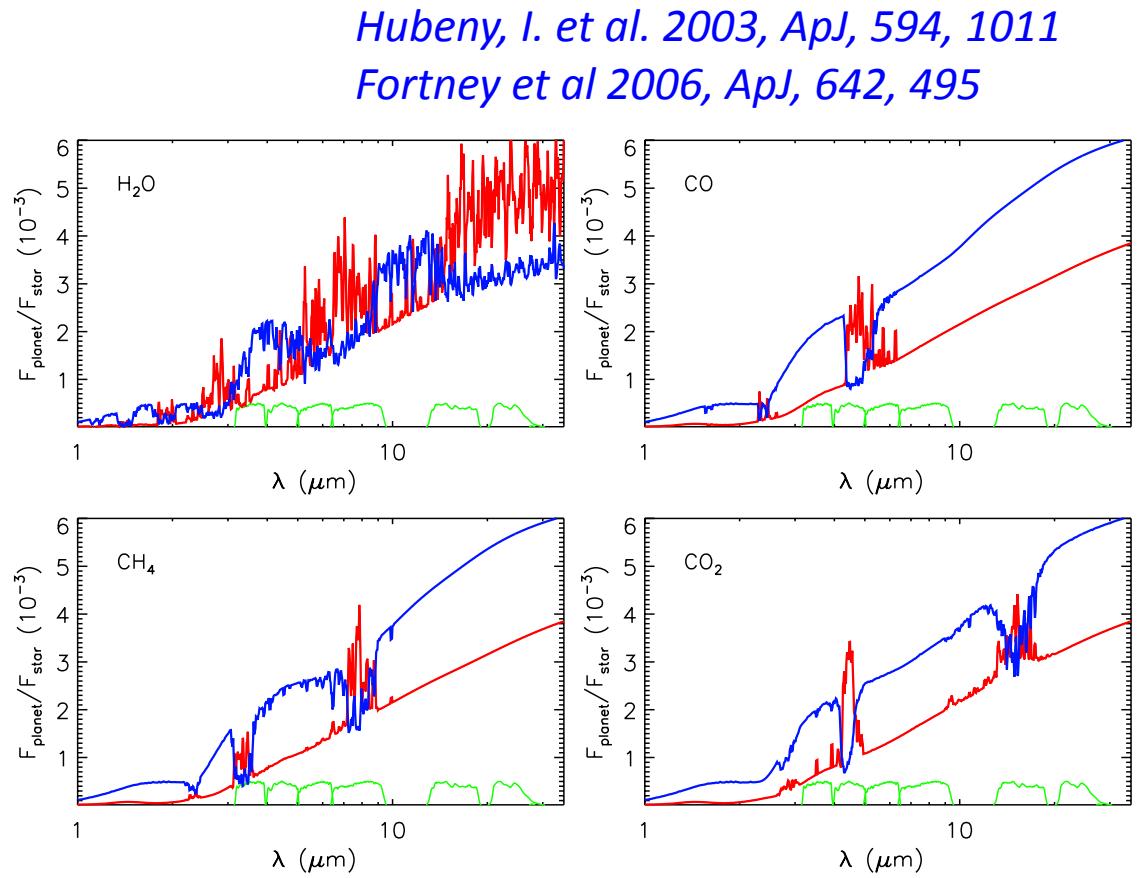
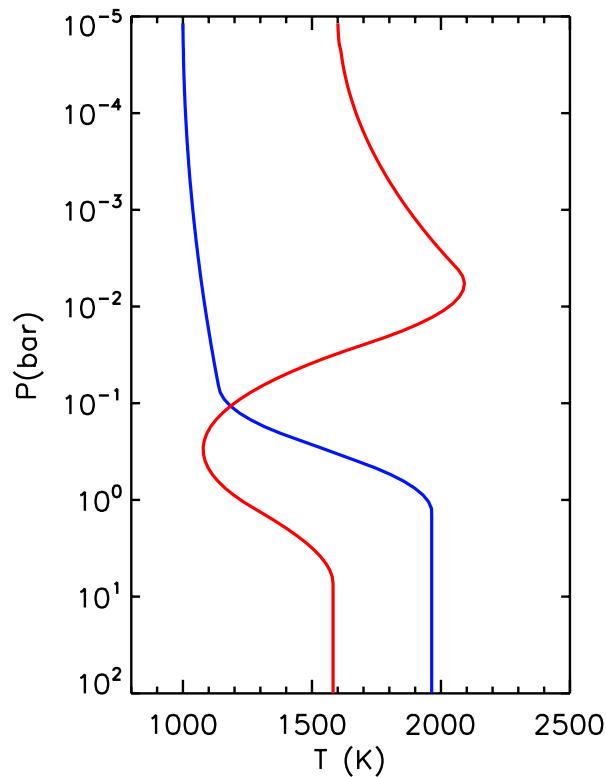


$$T(\tau) = T_{\text{eff}} \left[\frac{3\tau}{4} + \frac{1}{2} \right]^{1/4}$$

$$F = -\frac{16}{3} \frac{\sigma T^3}{\kappa \rho} \frac{dT}{dz} = \frac{16\sigma T^3}{3} \frac{dT}{d\tau}$$

Thermal inversions in hot Jupiters (The TiO/VO Hypothesis)

TiO and VO can be very strong absorbers of incident stellar irradiation in the visible high in the atmospheres of hot Jupiters, and can hence cause thermal inversions.



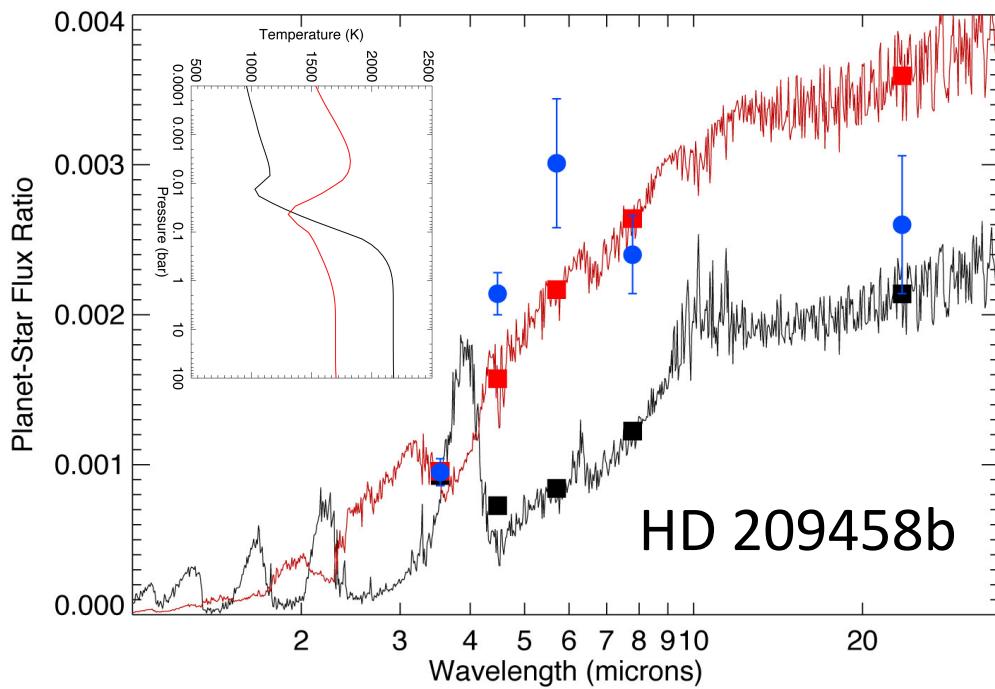
Madhusudhan & Seager 2010

Hubeny, I. et al. 2003, ApJ, 594, 1011

Fortney et al 2006, ApJ, 642, 495

Thermal inversions in hot Jupiters

Classification of hot Jupiter atmospheres

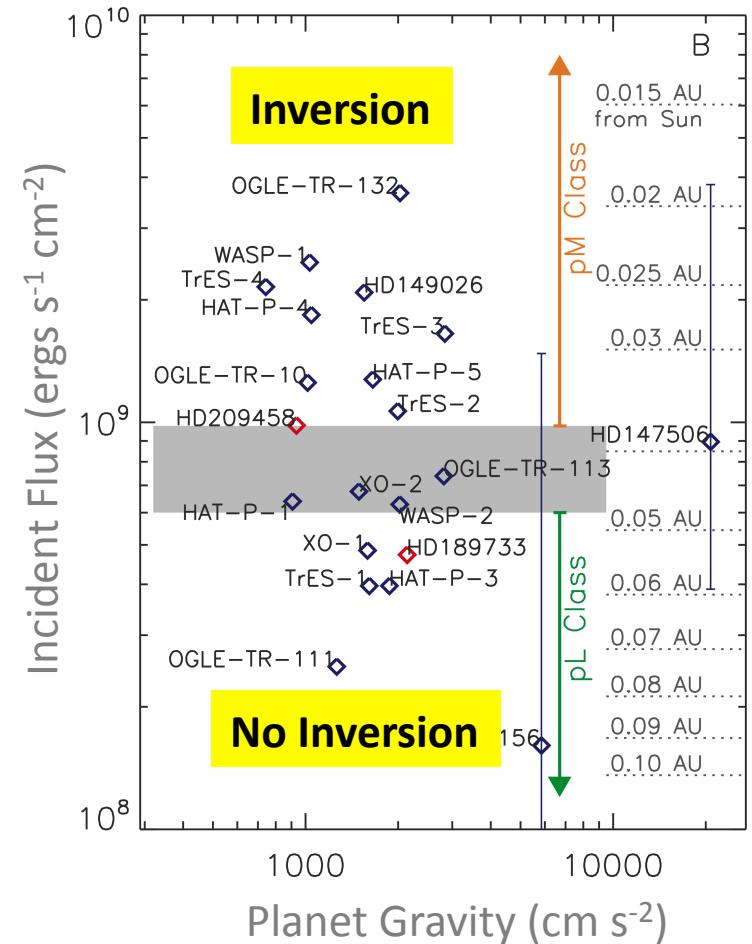


Data: [Knutson et al. 2008, ApJ, 673, 526](#)

Models: [Burrows et al. 2007, ApJ, 668, L171](#)

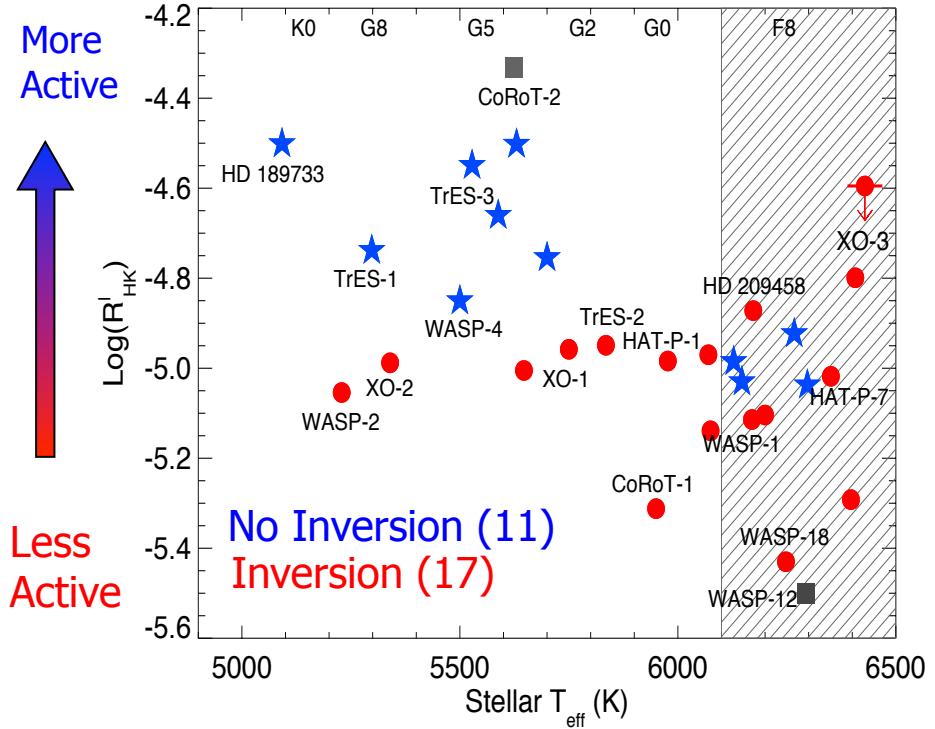
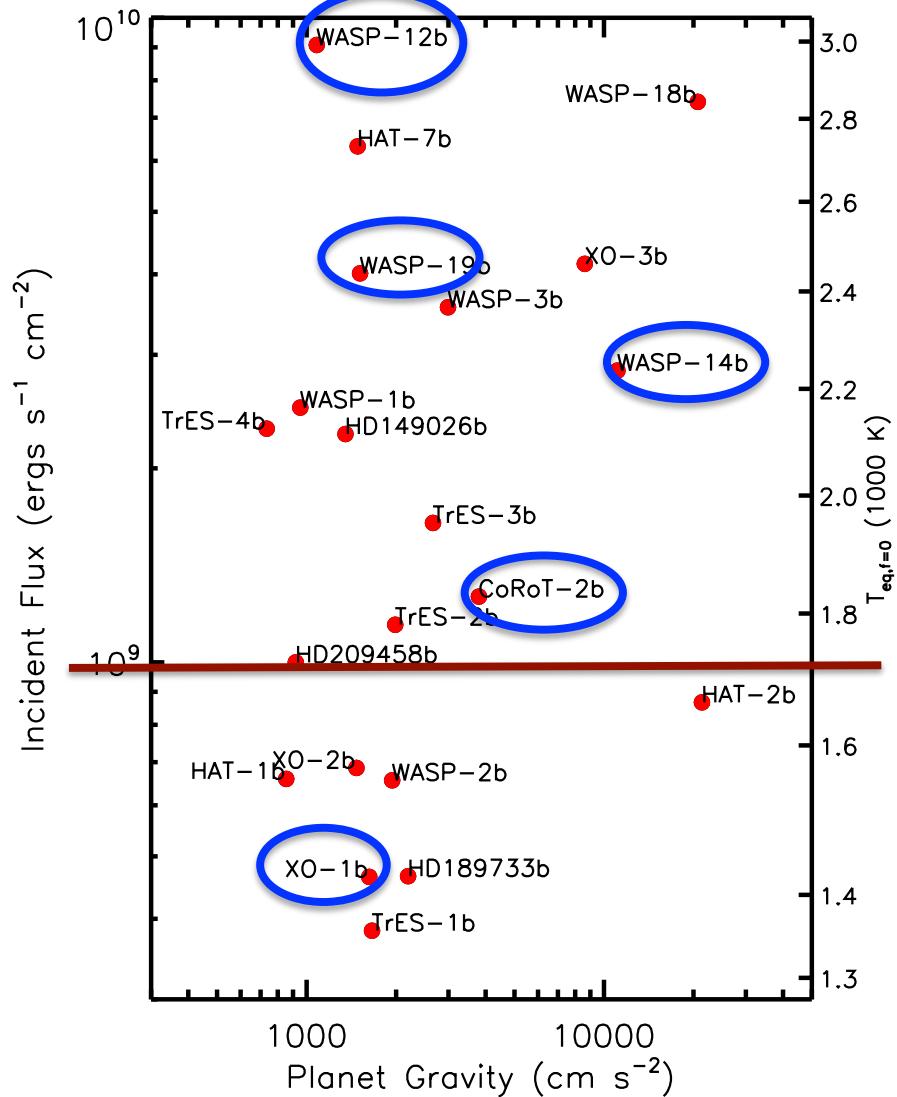
But, TiO and VO may be depleted due to gravitational settling and condensation

[Spiegel et al. 2009, ApJ, 699, 1487](#)



[Fortney et al. 2008, ApJ, 678, 1419](#)

Classifications of hot Jupiters

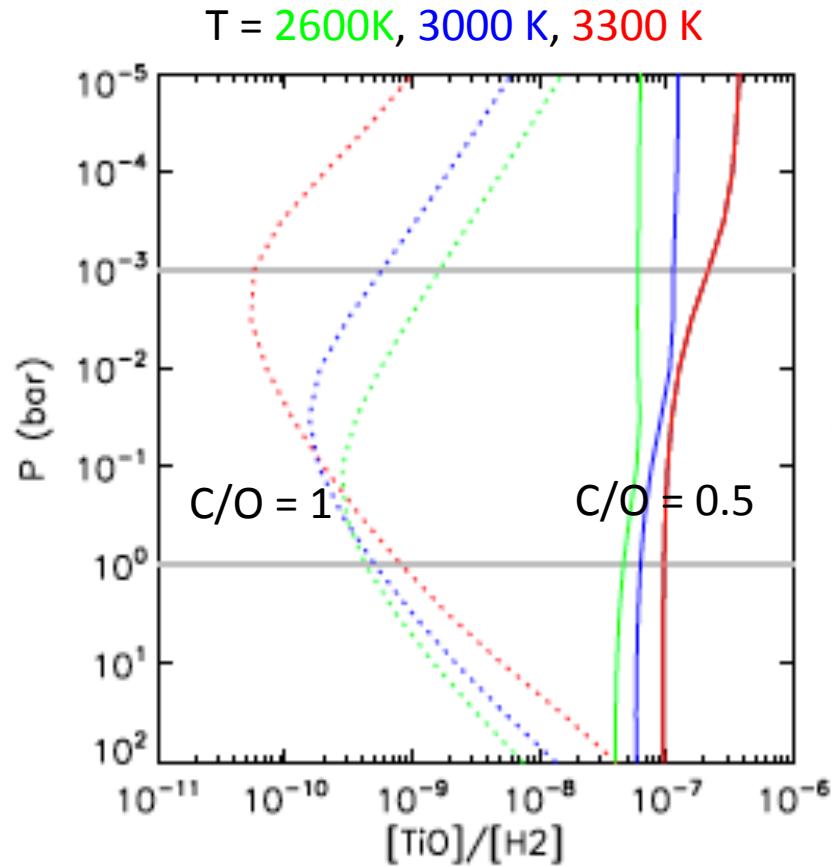


Correlation Between Stellar Activity and Temperature Inversions

Knutson et al. 2010, ApJ, 720, 1569

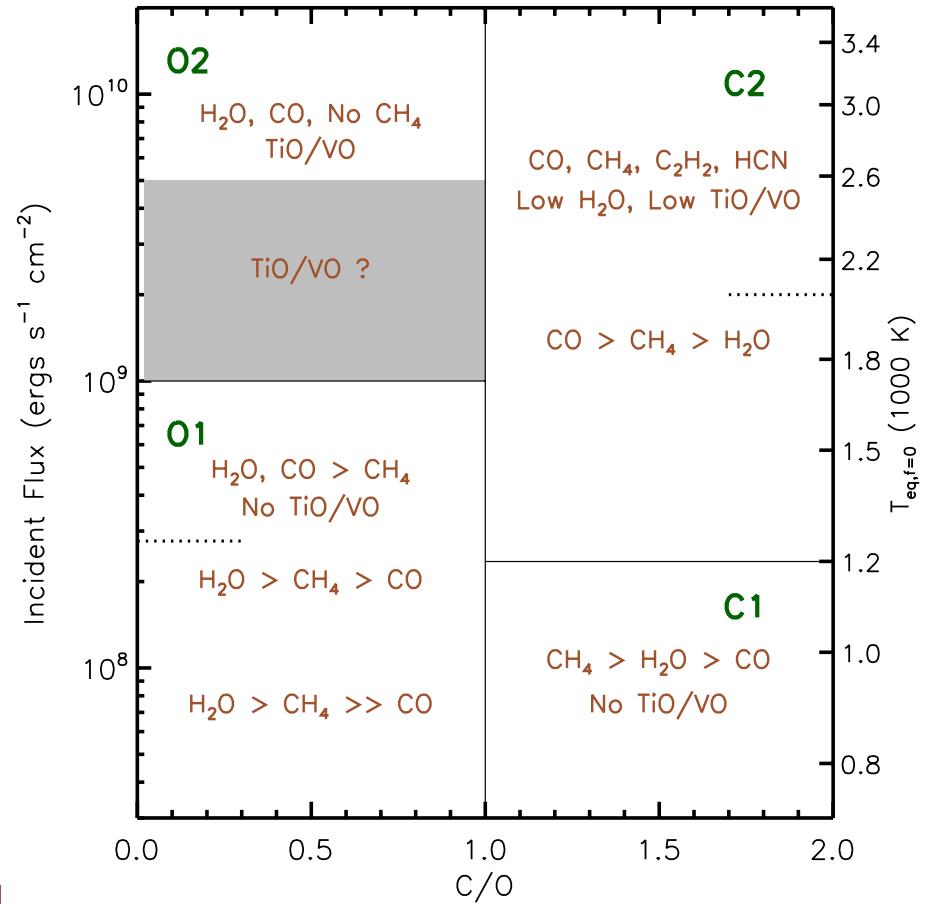
Machalek et al. 2008; Fressin et al. 2010; Deming et al. 2010;
Anderson et al. 2012; Blecic et al. 2013

Classifications of hot Jupiters



TiO and VO can be 100x lower for $C/O \geq 1$.

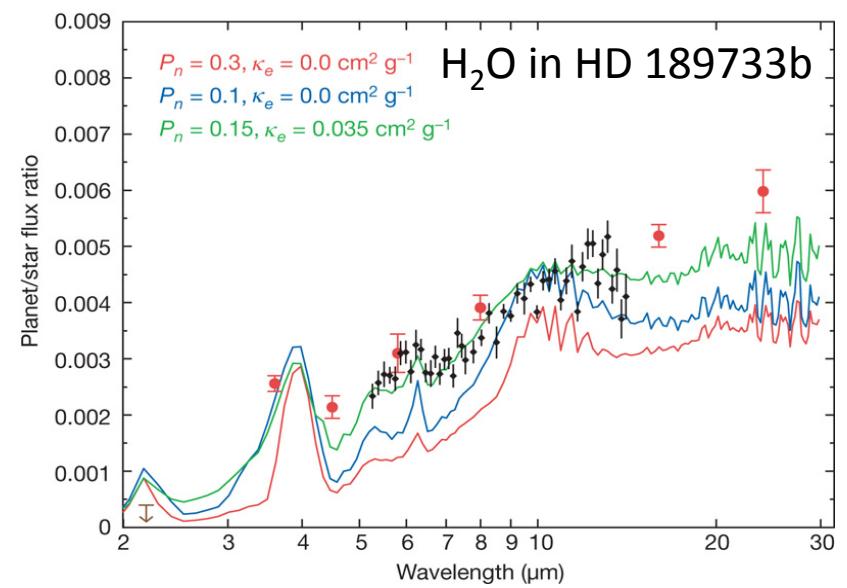
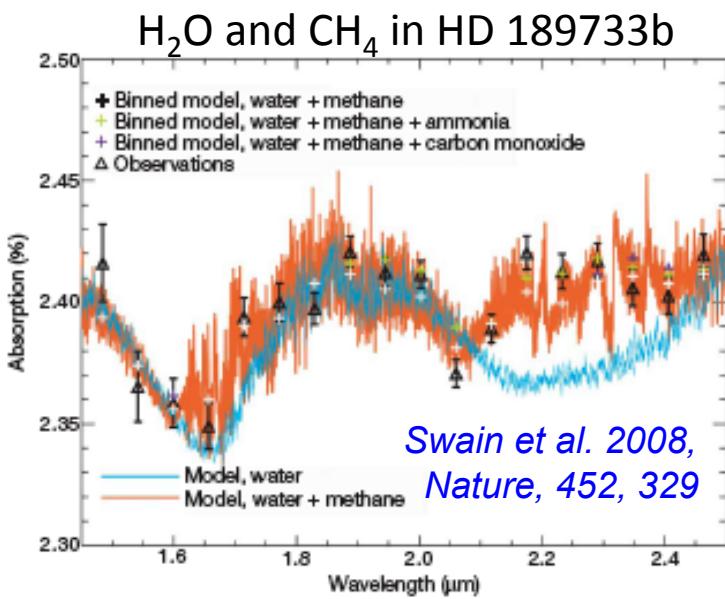
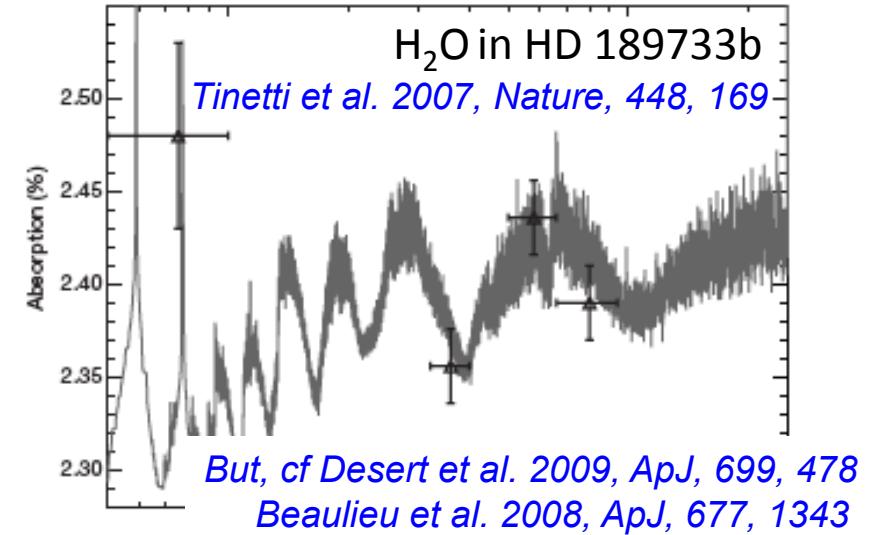
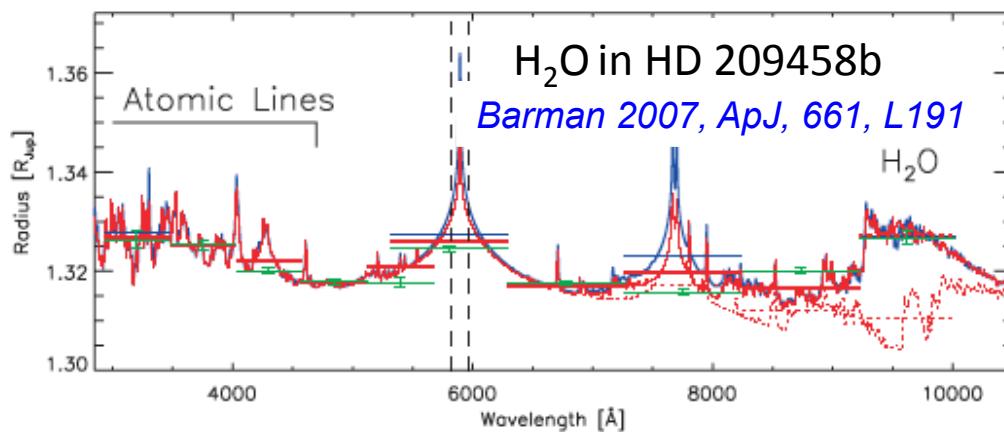
Madhusudhan et al. 2011, ApJ, 743, 191



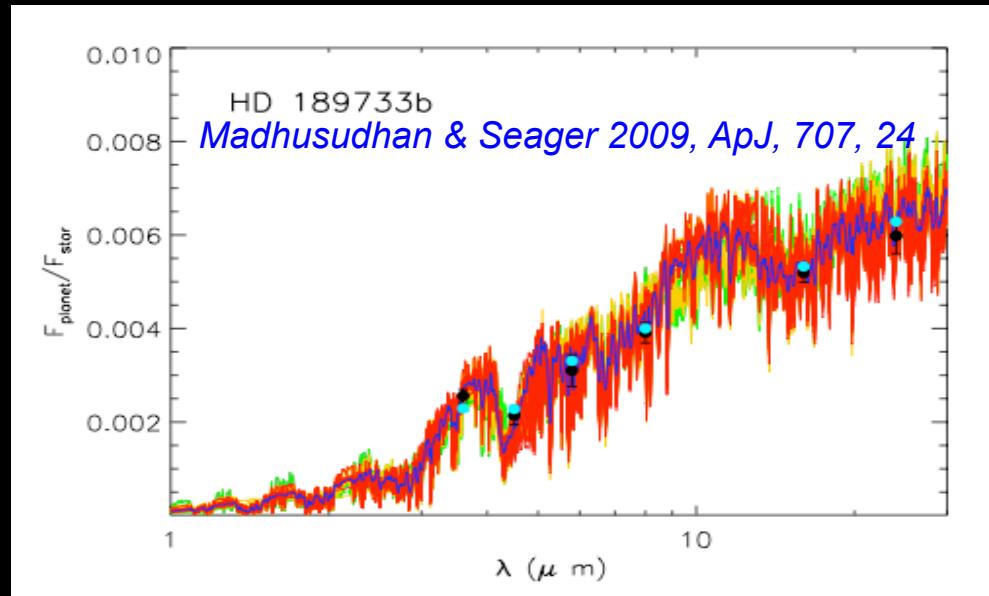
2-D classification scheme with C/O ratio as second dimension

Madhusudhan 2012, ApJ, 758, 36

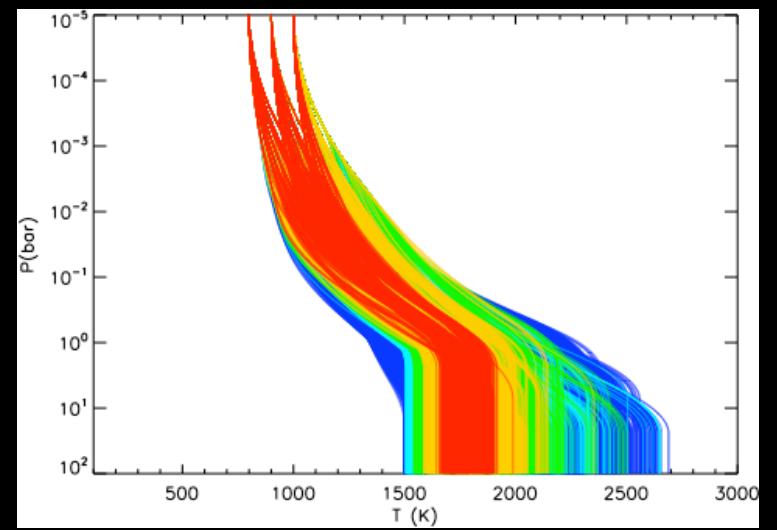
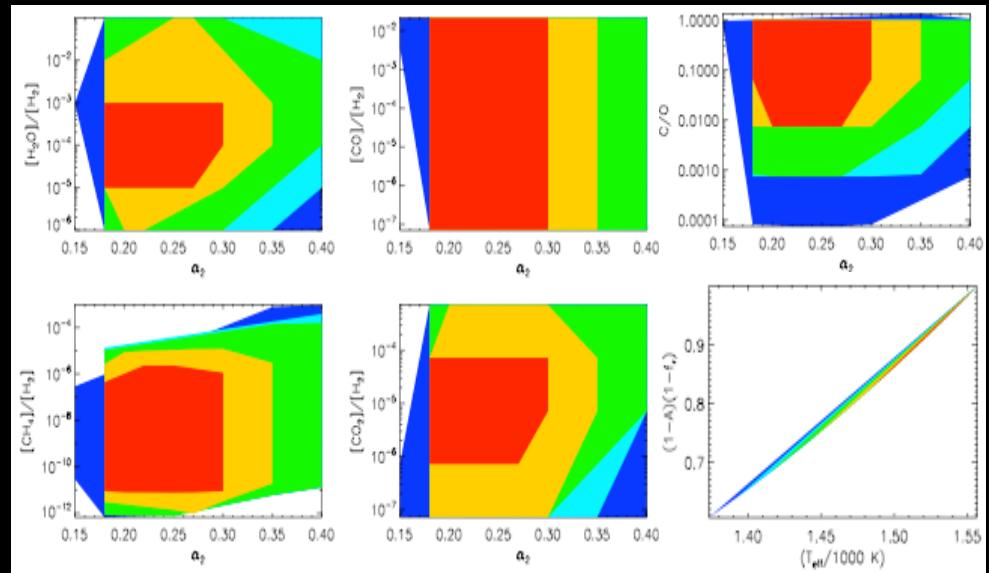
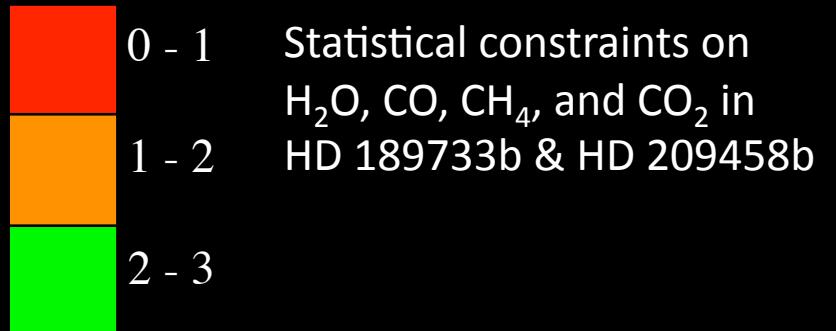
Molecular inferences in hot Jupiter Atmospheres



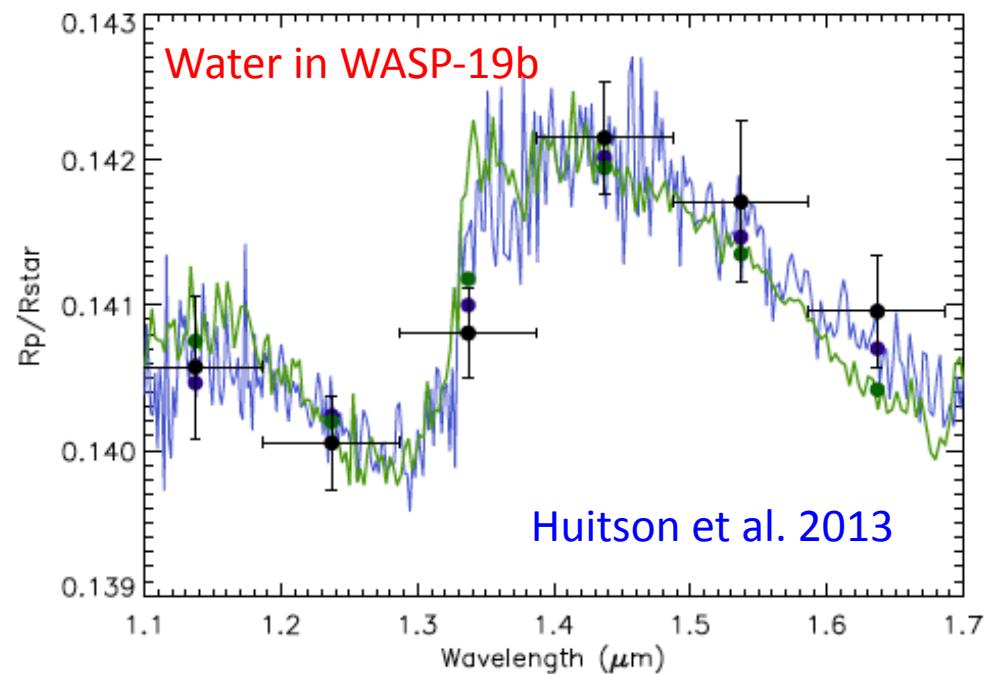
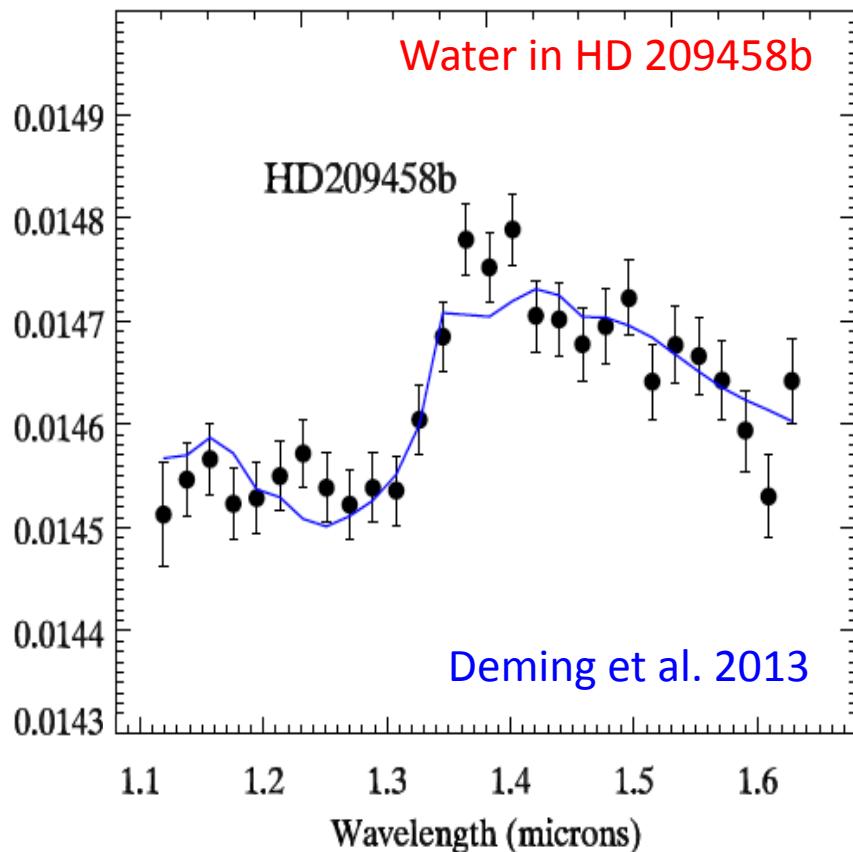
Atmospheric Retrieval for Exoplanets



$$\xi^2 = \frac{1}{N_{\text{obs}}} \sum_{i=1}^{N_{\text{obs}}} \left(\frac{f_{i,\text{obs}} - f_{i,\text{model}}}{\sigma_i} \right)^2$$

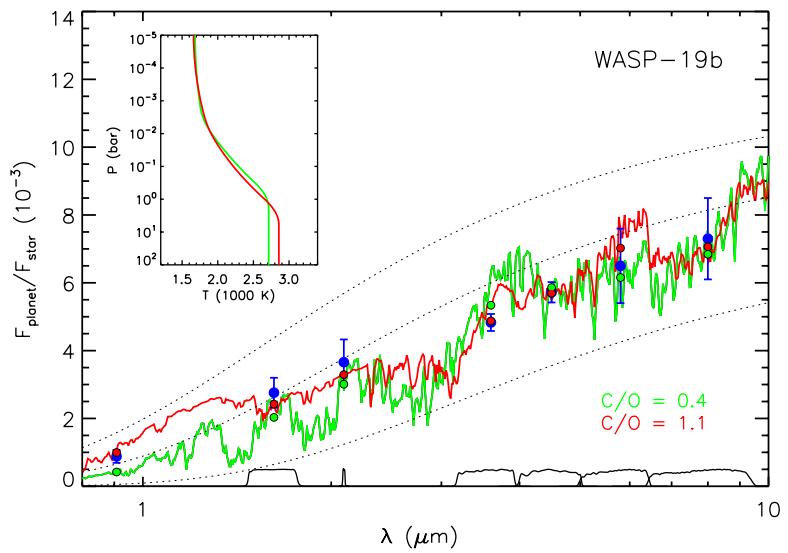


Other Examples of Molecular Inferences

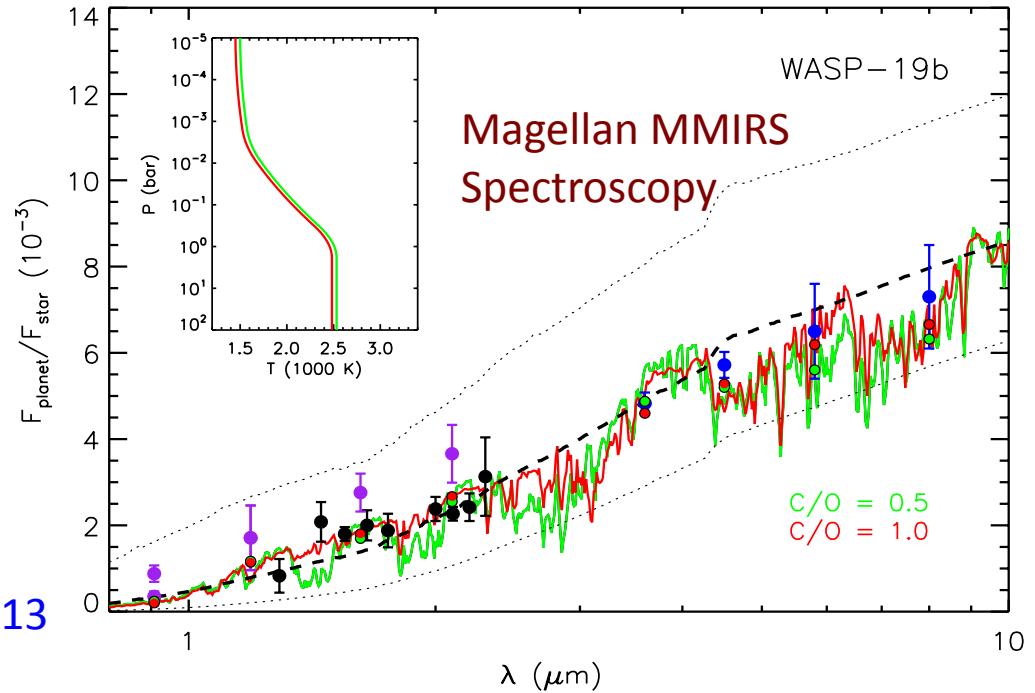


Also see Desert et al. 2009; Madhusudhan & Seager 2009; Swain et al. 2008, 2009; Tinetti et al. 2011; Madhusudhan & Seager 2011; Line et al. 2012; Lee et al. 2012; de Kok et al. 2013; Swain et al. 2013

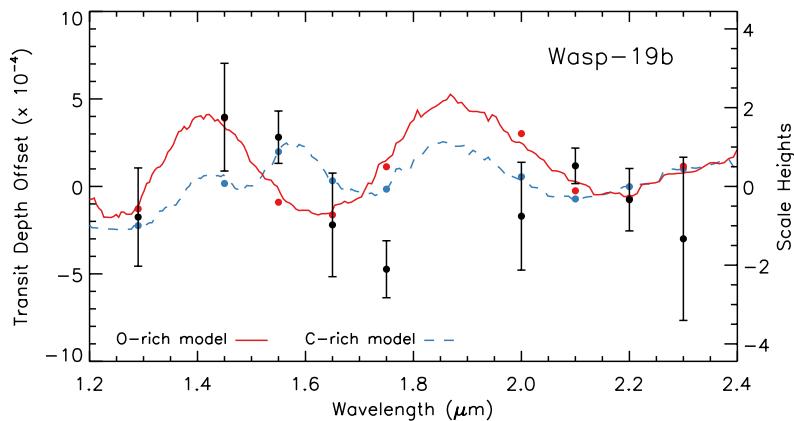
Ground-based Photometry and Spectra of hot Jupiters



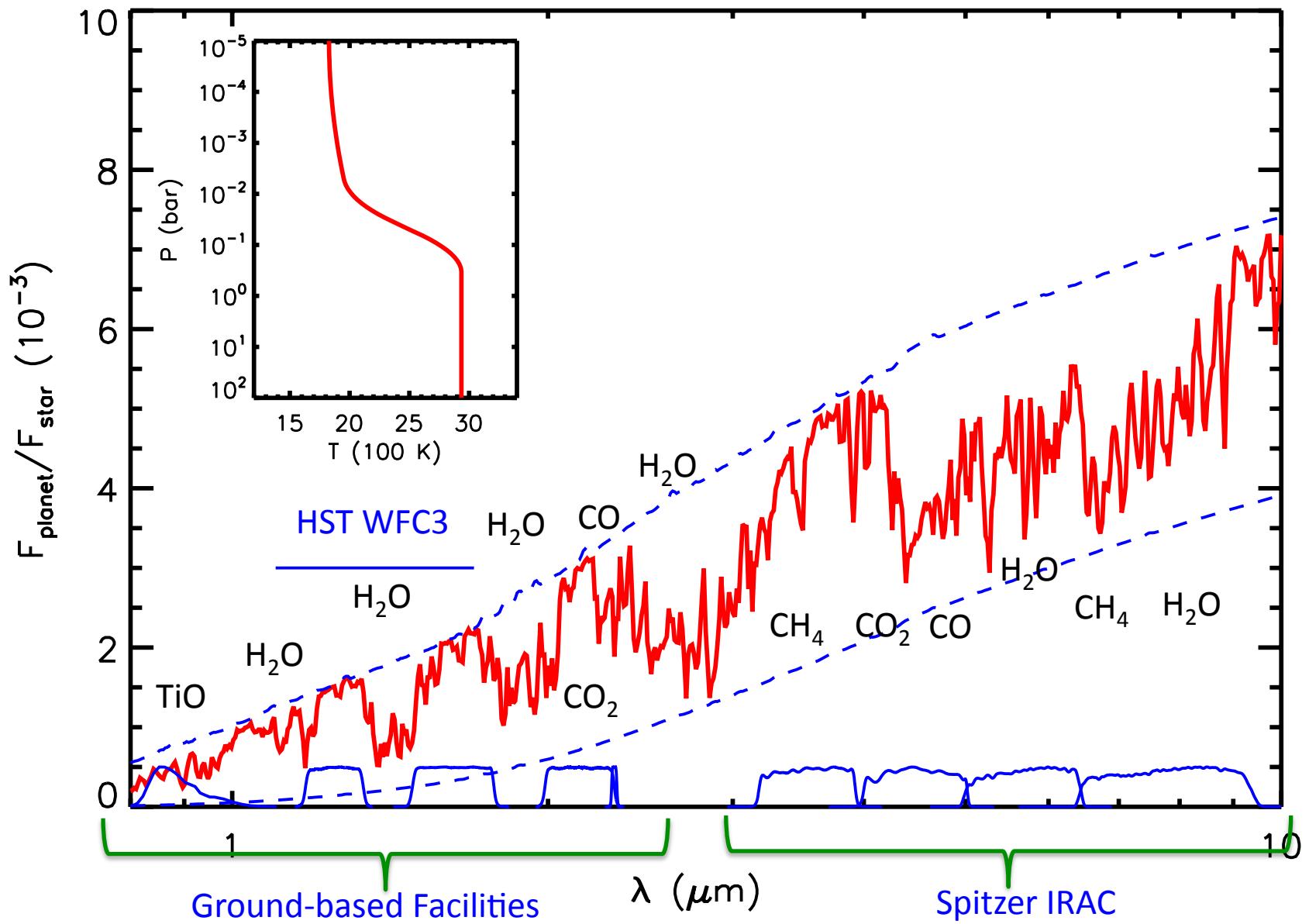
Anderson et al. 2012; Lendl et al. 2013



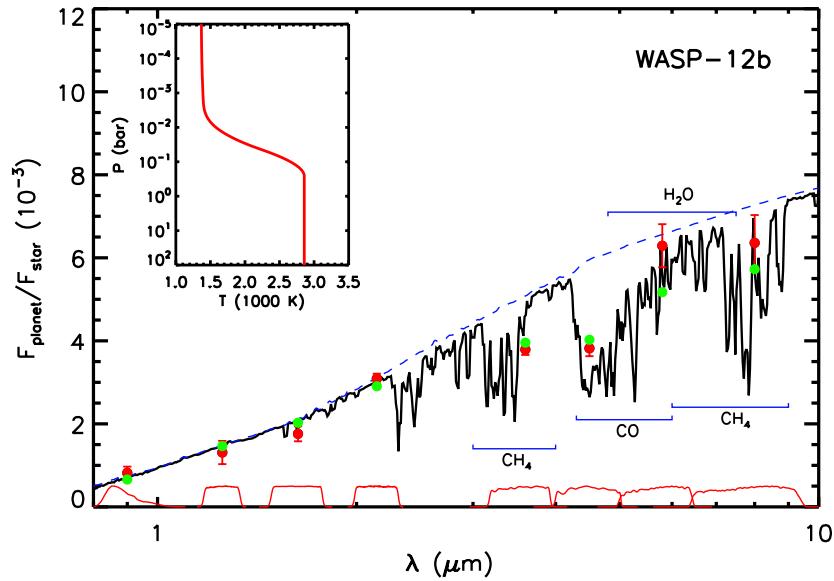
Bean et al. 2013



Spectral Signatures of hot Jupiter Atmospheres



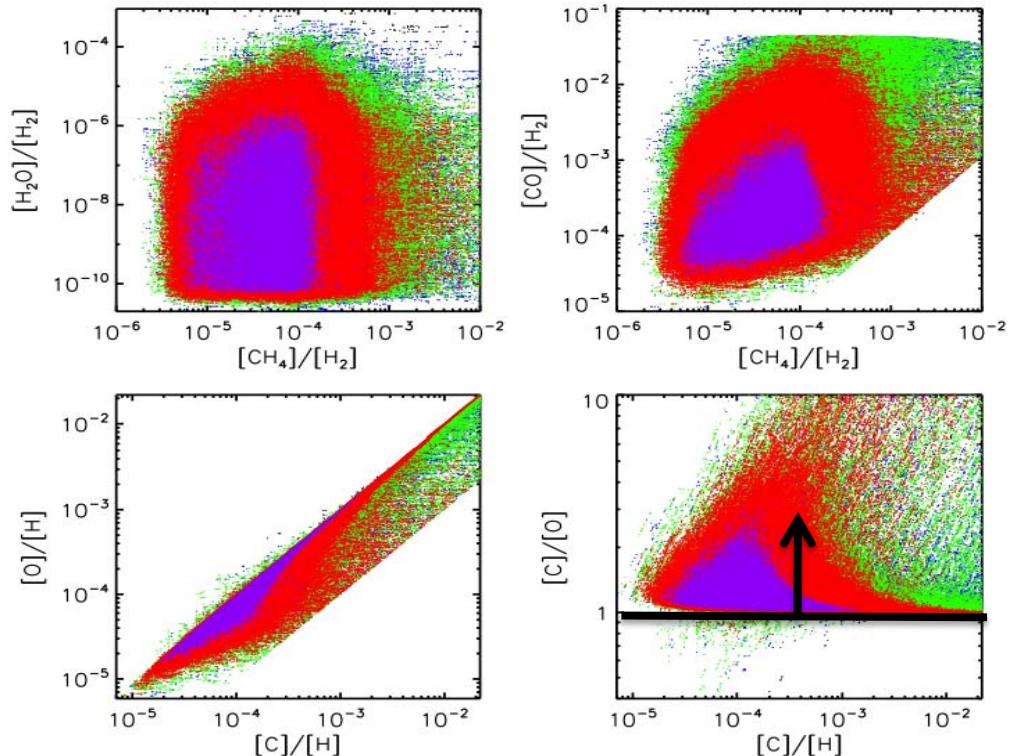
First measurement of atmospheric C/O in a giant planet



Key Molecular Constraints

- $\text{H}_2\text{O}/\text{H}_2 \leq 6 \times 10^{-6}$
- $\text{CH}_4/\text{H}_2 \geq 8 \times 10^{-6}$

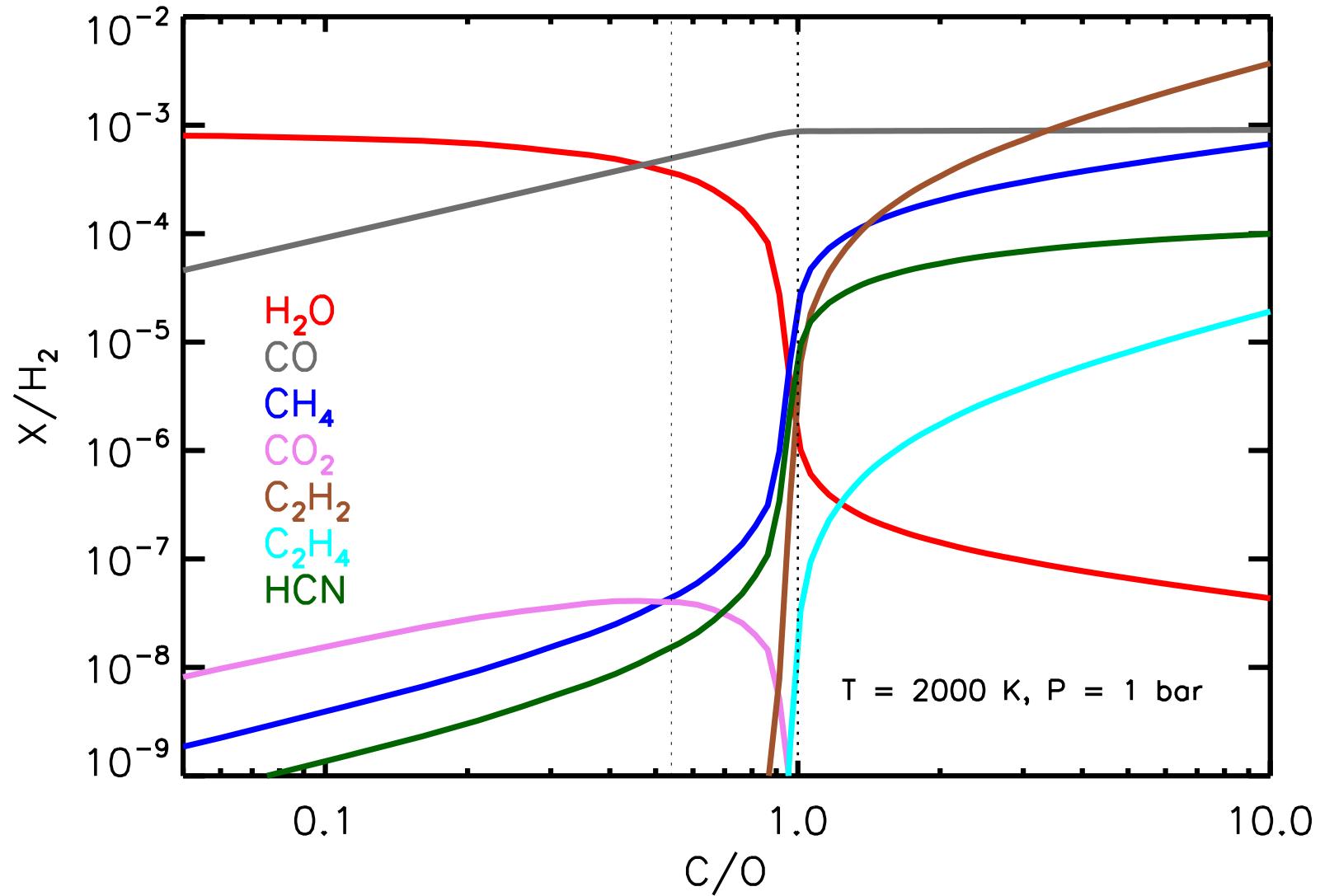
$\text{C}/\text{O} \geq 1$



*Adapted from Madhusudhan et al. 2011,
Nature, 469, 64*

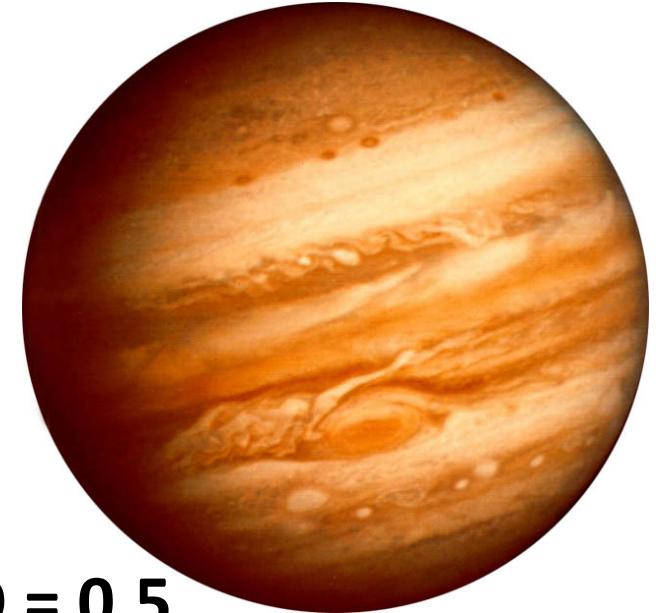
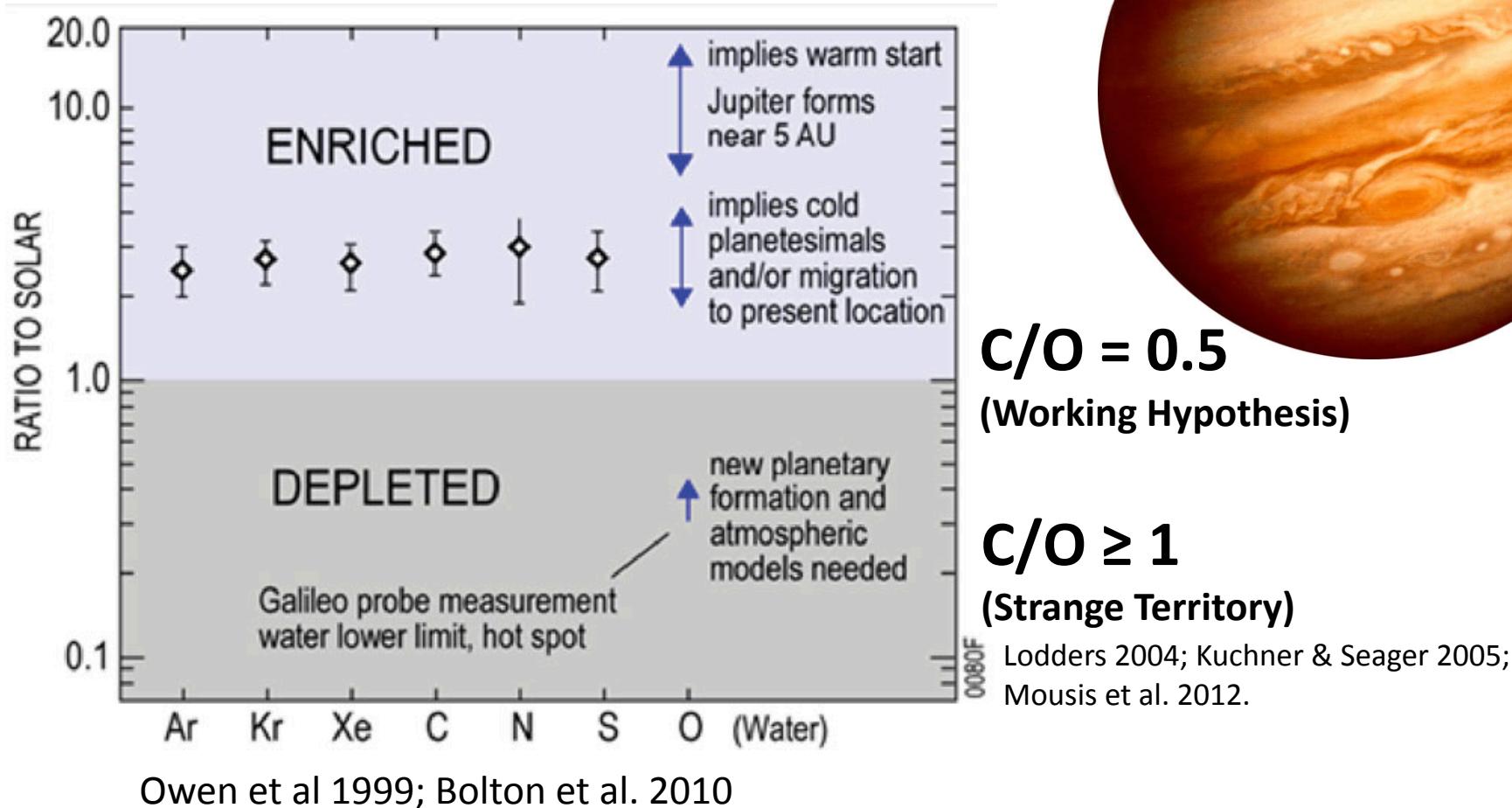
*Data from Lopez-Morales et al. 2010; Croll
et al. 2010; Campo et al. 2011
But cf Crossfield et al. 2012, Cowan et al. 2012,
Swain et al. 2012, Stevenson et al. 2013*

Influence of C/O on Atmospheric Chemistry



Madhusudhan 2012, ApJ, 758, 36

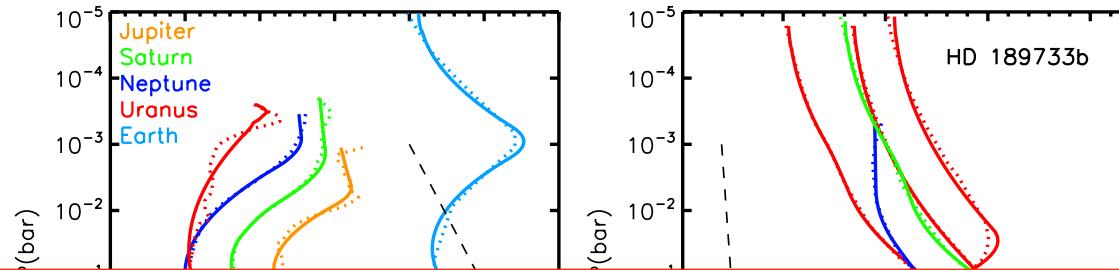
Atmospheric abundances in Jupiter



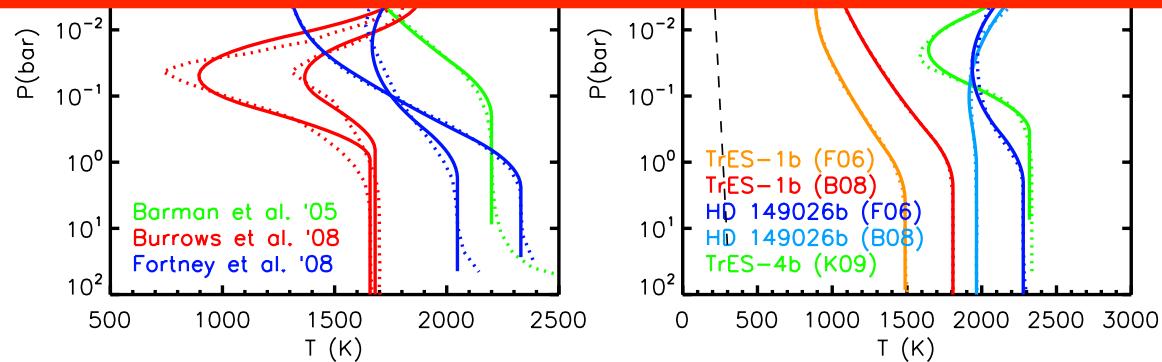
Key Message: We don't know the O/H and C/O ratios in the giant planets in the solar system

The Juno mission (@ Jupiter in 2016) aims to determine the water content, and hence O/H, in Jupiter's atmosphere.

Temperature Profiles of Planetary Atmospheres

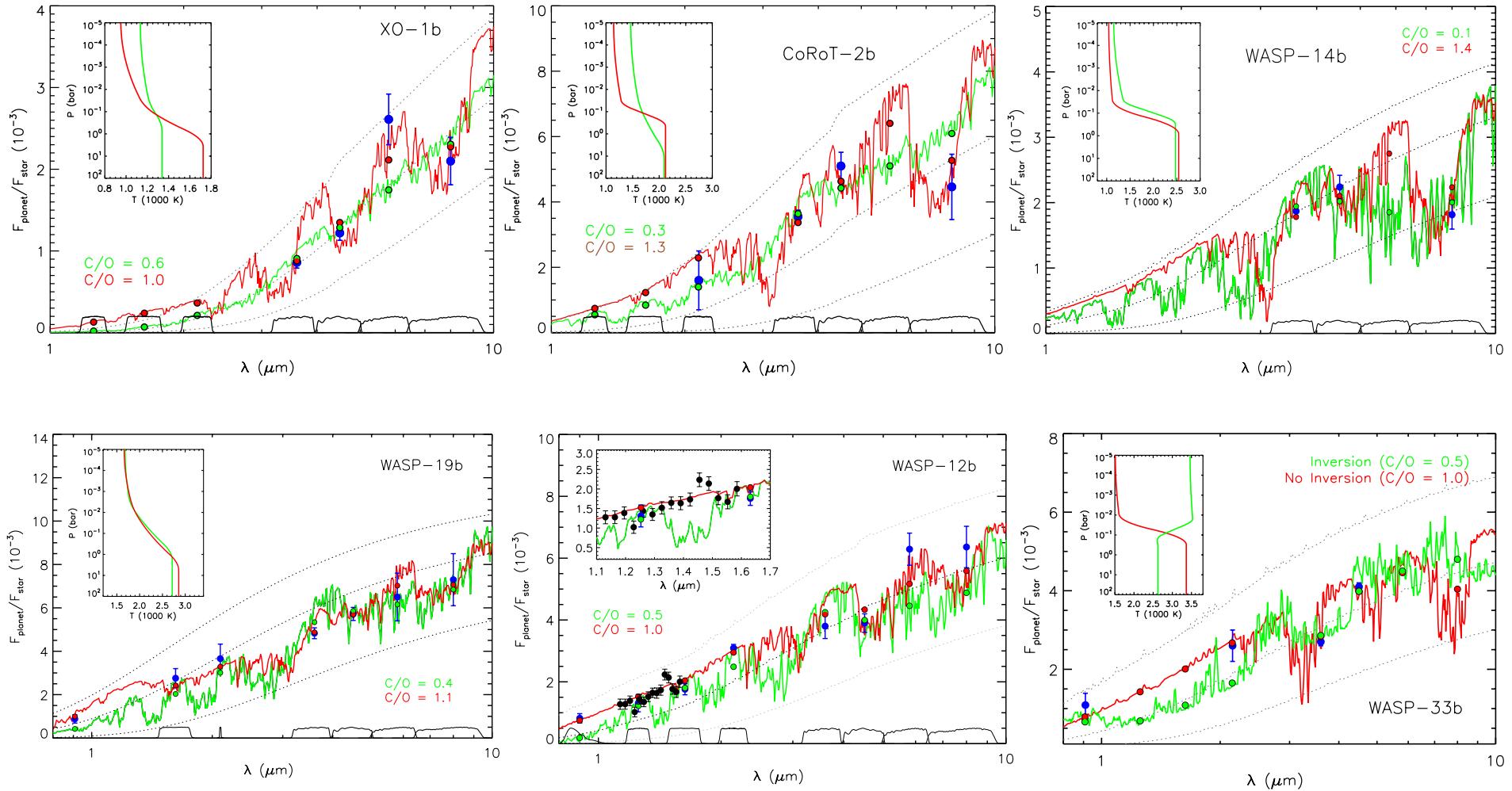


We can measure O/H and C/O ratios
in hot Jupiters better than we can
on Jupiter!



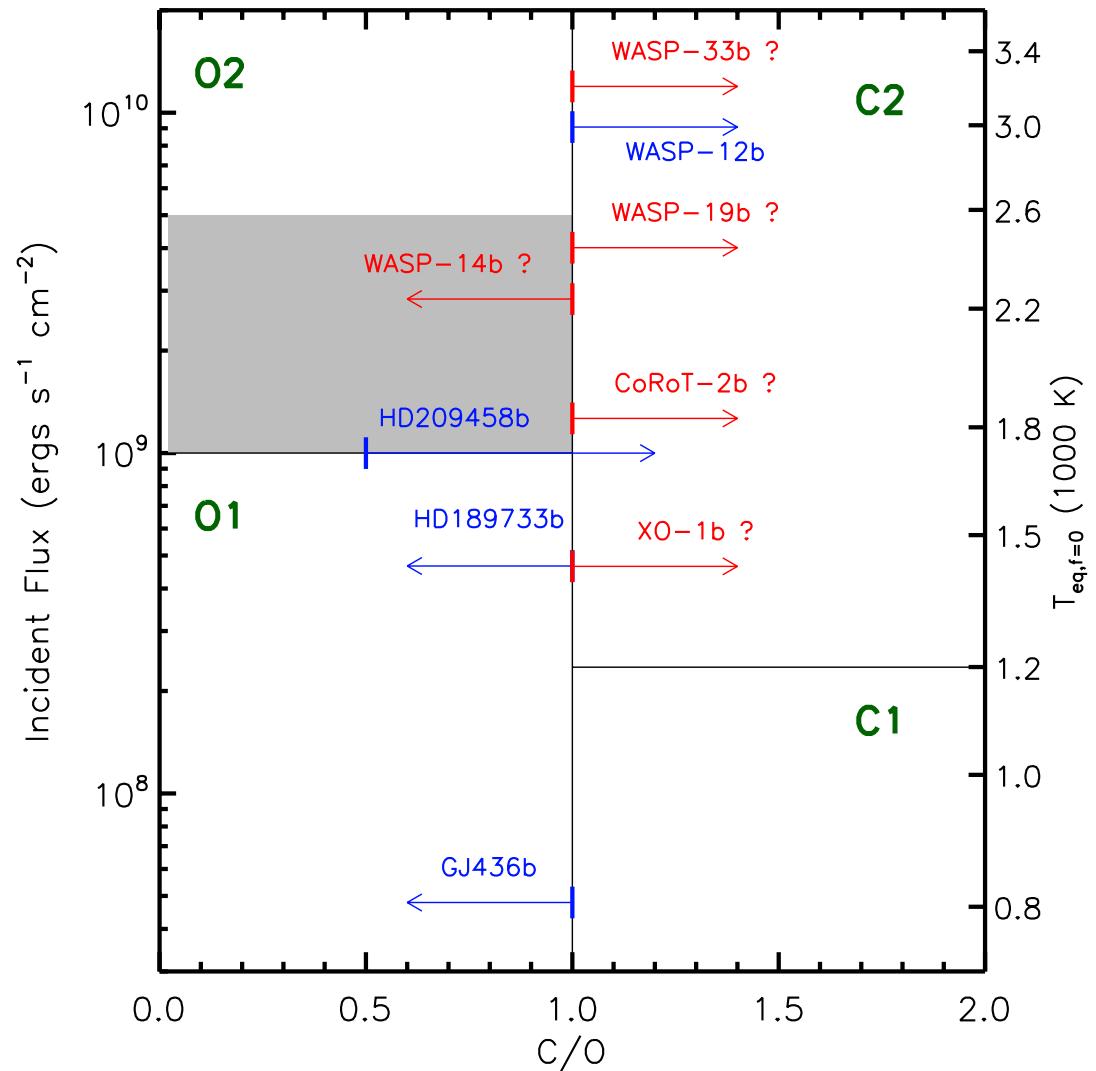
Madhusudhan & Seager 2009

C/O ratios in Exoplanetary Atmospheres



Madhusudhan 2012, ApJ, 758, 36

C/O Ratios in Hot Jupiter Atmospheres



Madhusudhan 2012, ApJ, 758, 36

Implications for Planet Formation

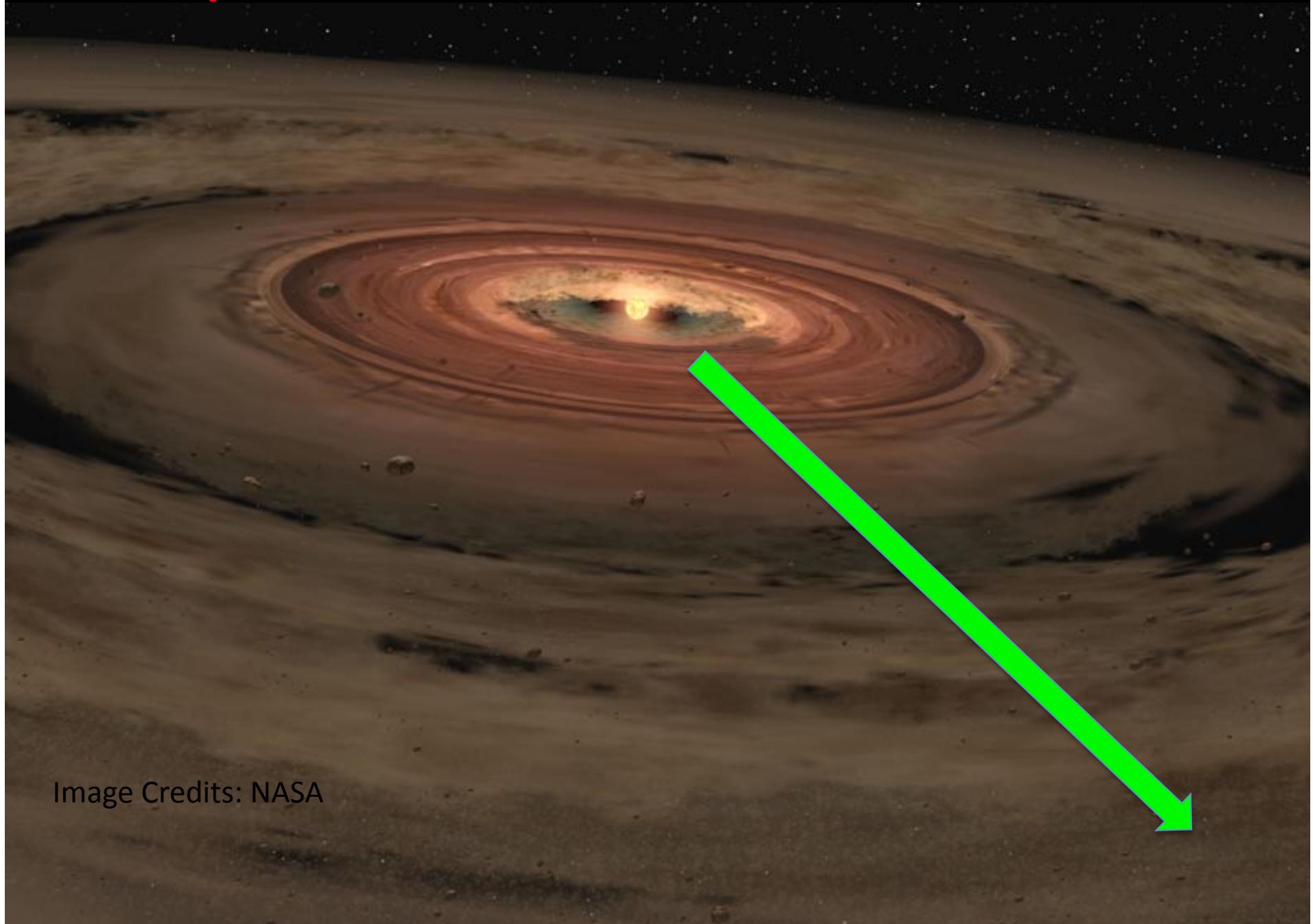
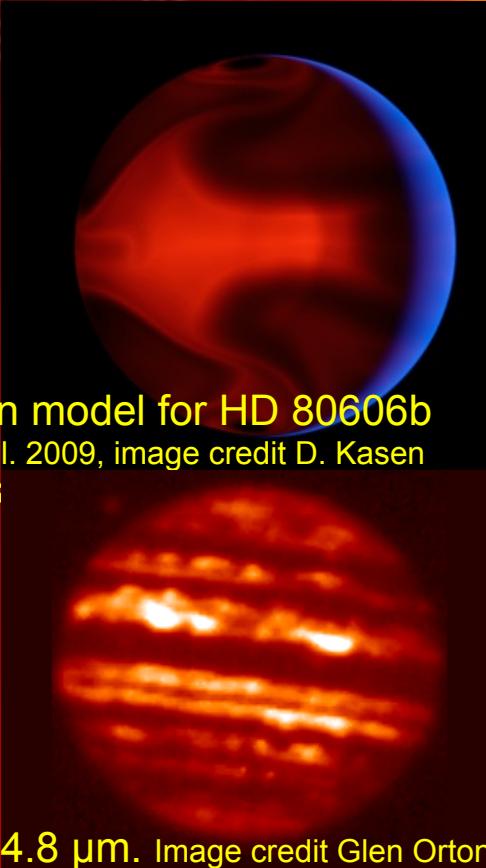


Image Credits: NASA

Atmospheric Circulation on Hot Jupiters



Hot Jupiters should be **tidally locked**, may have large thermal and/or chemical gradients between the two hemispheres.

Planet's slow rotation means that the circulation should be **global in scale** (broad jets, large vortices).

Cho et al. 2008

Laughlin et al. 2009

Showman et al. 2009

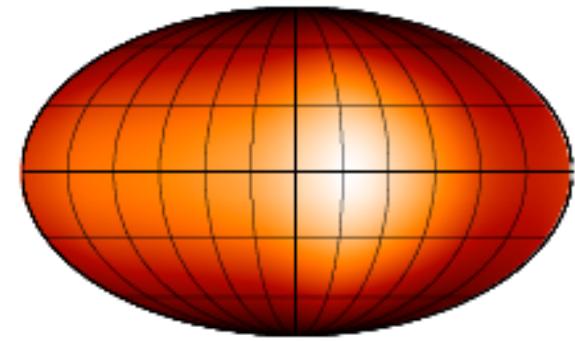
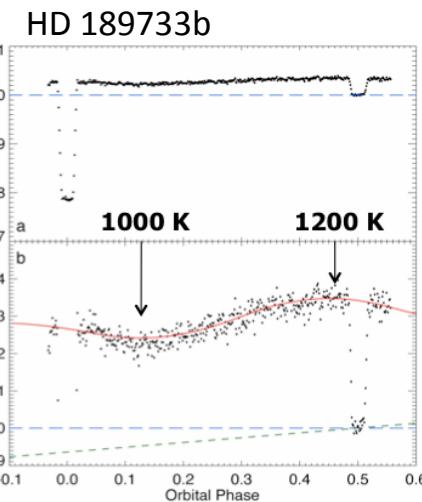
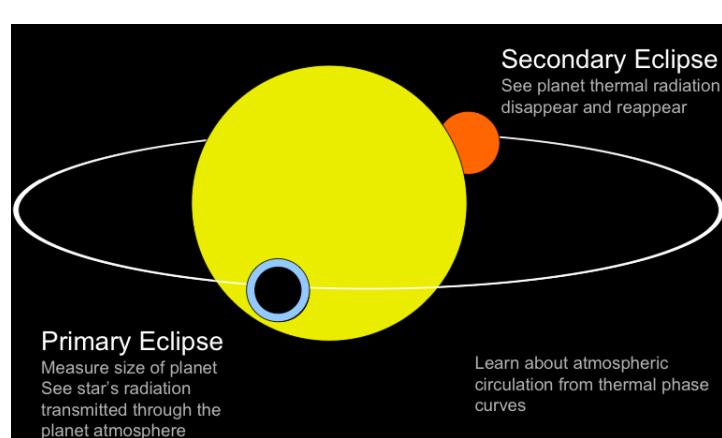
Heng et al. 2011

Rauscher & Menou 2012

Dobbs-Dixon et al. 2012

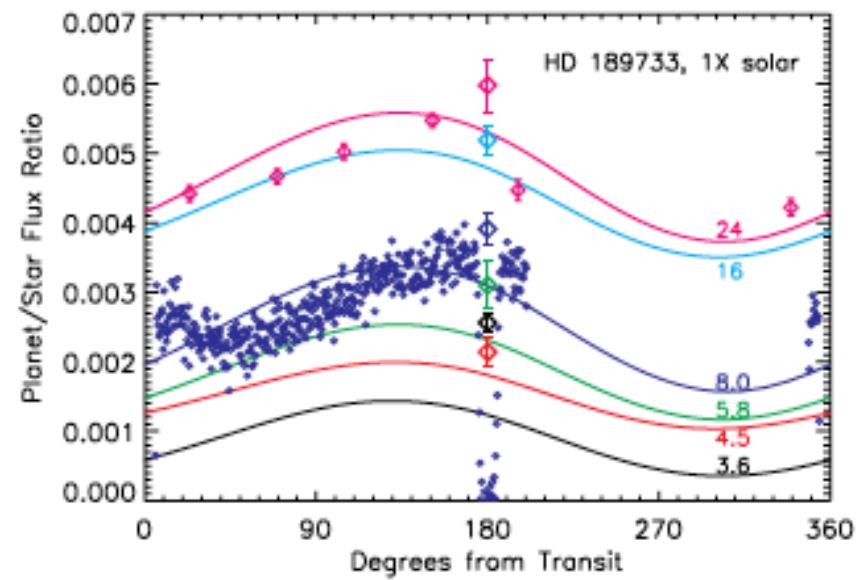
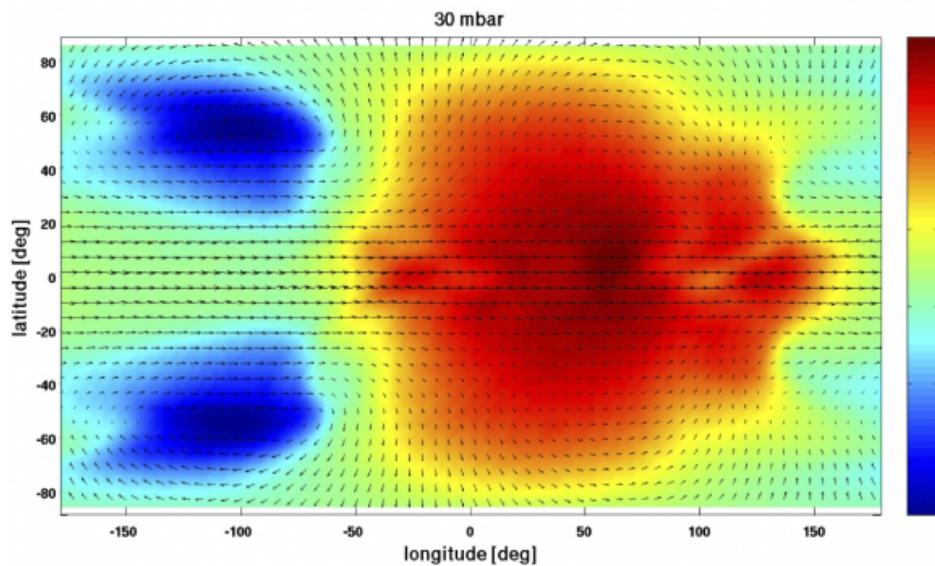
Image credit: ESA/C. Carreau

Thermal Phase Curves and Atmospheric Dynamics



*Knutson et al. 2007, 447, 183
Knutson et al. 2009, 690, 822*

Cowan & Agol 2008, ApJ, 678, L129



Showman et al. 2009, ApJ, 678, 1419

3D GCM Models predict eastward shift of the hot spot away from the sub-stellar point, consistent with observations of phase curves.

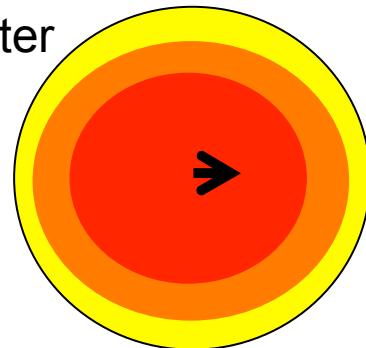
Atmospheric Circulation Models 101

To 0th order, response of atmosphere to radiative forcing depends on two parameters:

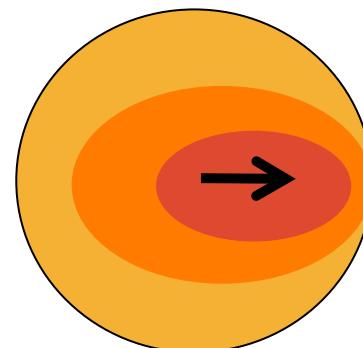
- *Radiative* time scale t_R set by atmospheric opacity (metallicity, chemistry)
- *Advection* time scale t_A set by wind speed, rotation rate

Day-night temperature gradient on tidally locked planets depends on ratio of *radiative* to *advection* time scales at photosphere

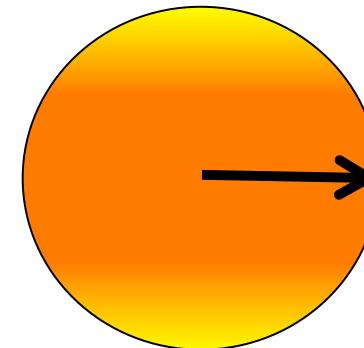
Hot Jupiter
Dayside



$$t_R/t_A \ll 1$$



$$t_R/t_A \sim 1$$



$$t_R/t_A \gg 1$$

Hot Planets Have Hotter Day Sides

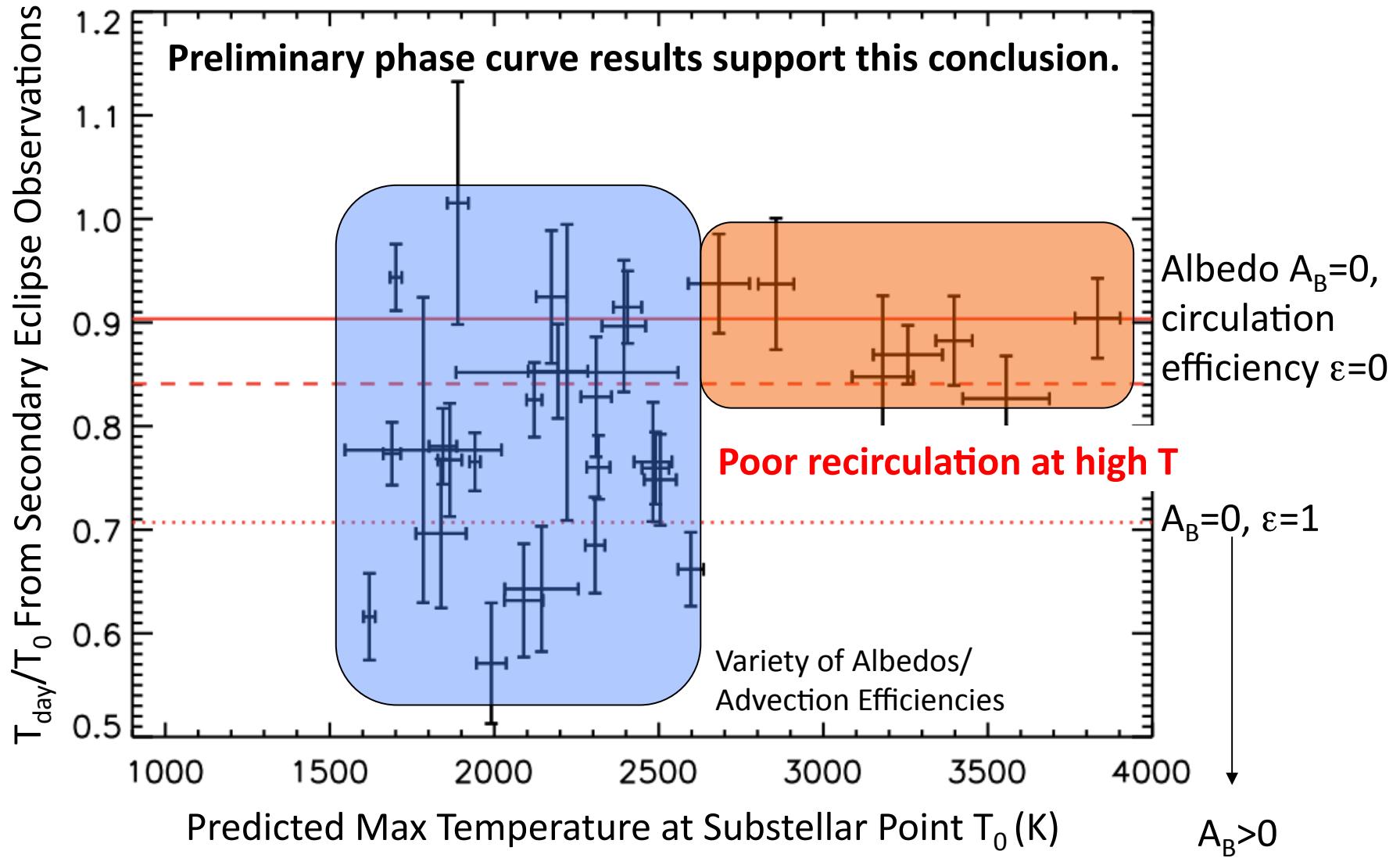
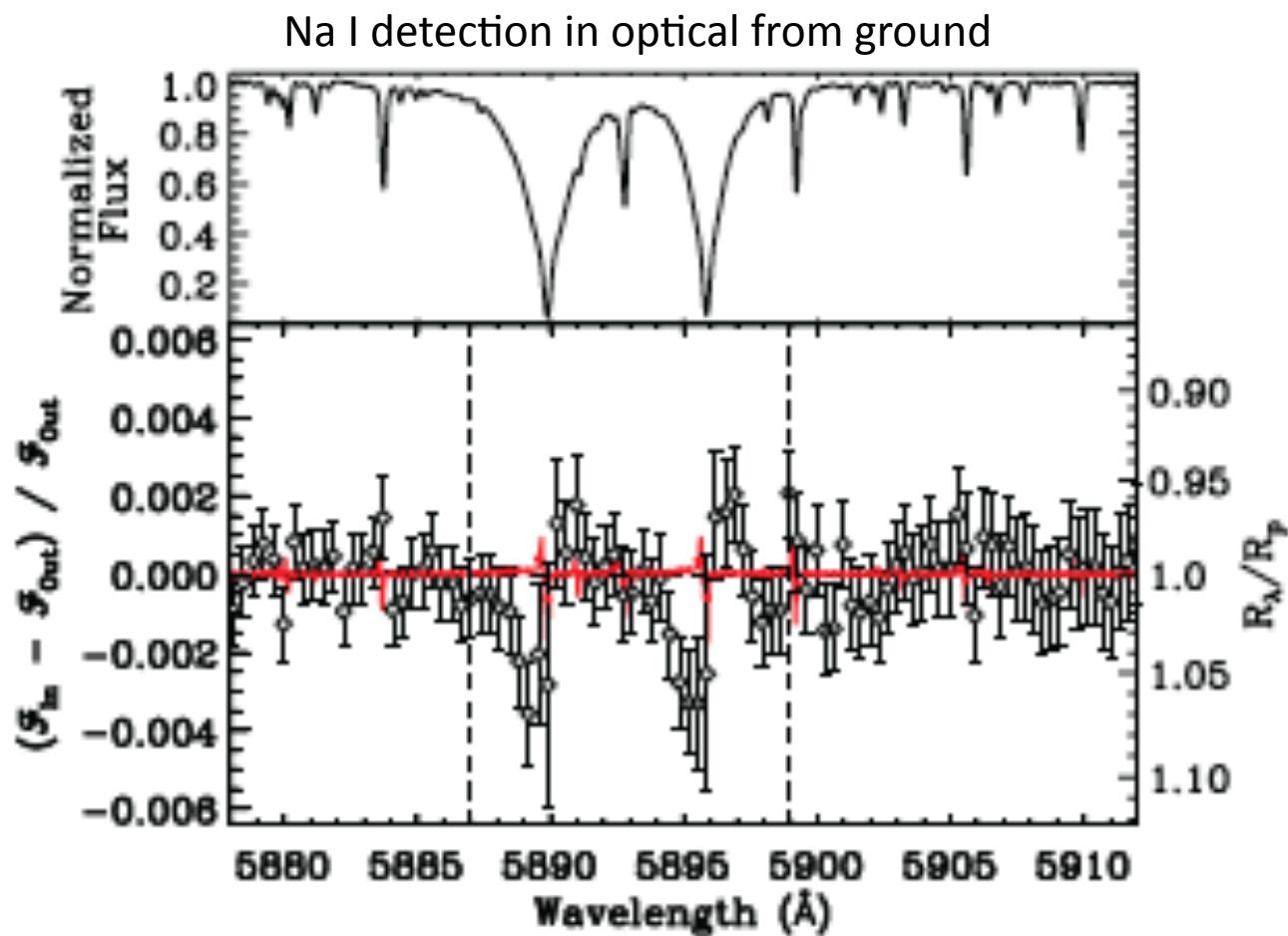


Figure courtesy N. Cowan, updated from Cowan & Agol (2011b)

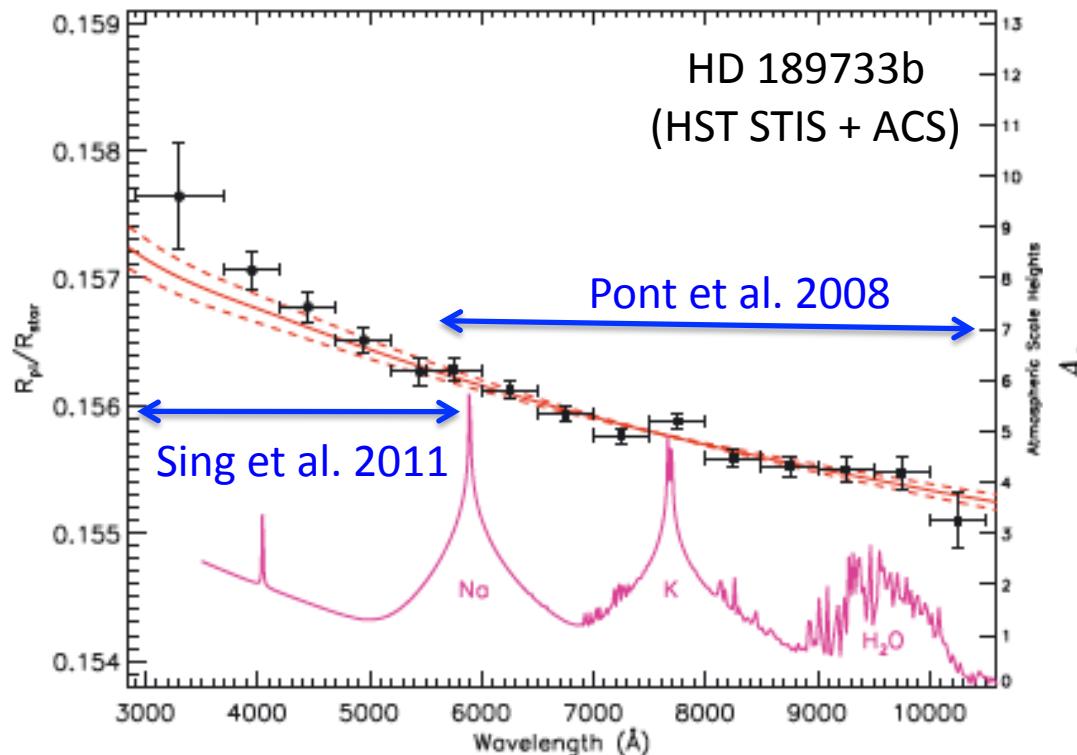
Inferences of Atomic Species in hot Jupiters



Redfield et al. 2008, ApJ, 673, L87

Charbonneau et al. 2002; Vidal-Madjar et al. 2003, 2004; Redfield et al. 2008; Snellen et al. 2008; Des Etangs et al. 2010; Wood et al. 2011; Colon et al. 2010; Sing et al. 2011.

Hazes and Clouds in hot Jupiter Atmospheres



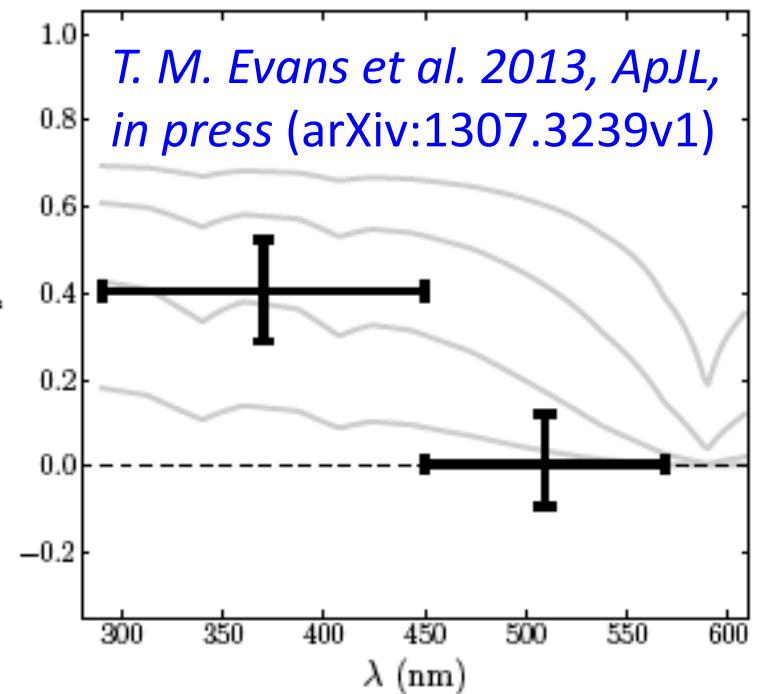
F. Pont et al. 2008, MNRAS, 385, 109

D. K. Sing et al. 2011, MNRAS, 416, 1443

Modeling and Theory:

Lecavelier Des Etangs et al. 2008, A&A, 481, L83

Helling et al. 2008, A&A, 485, 547

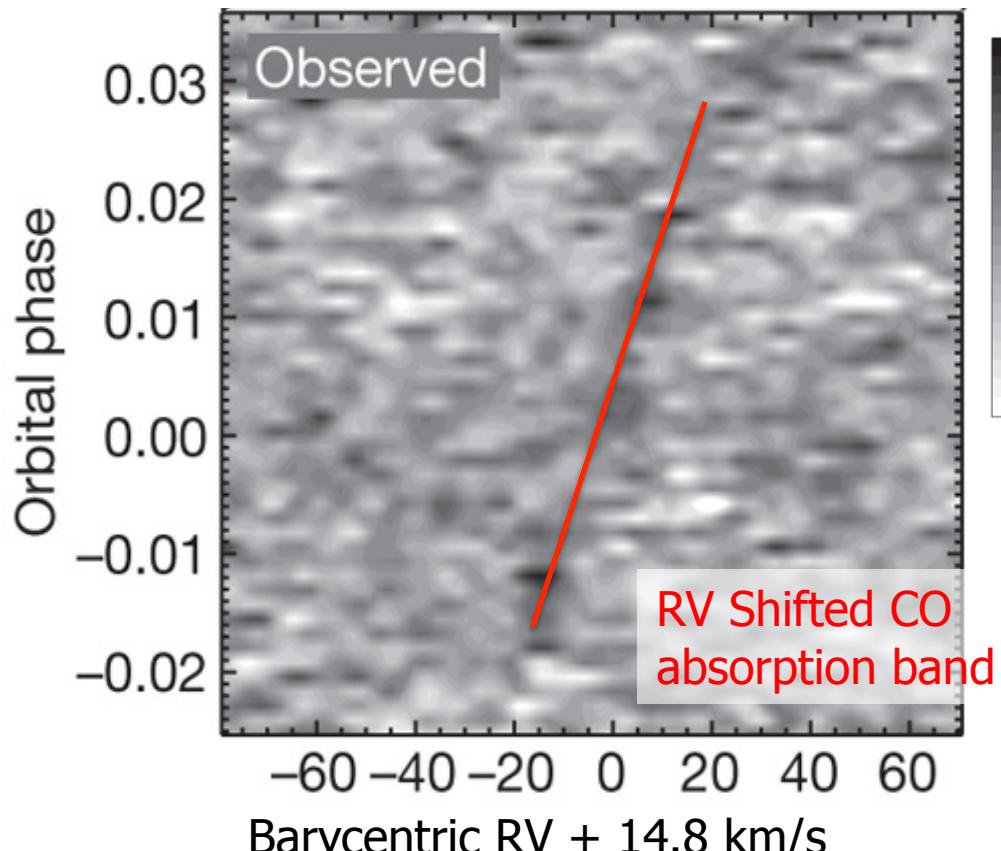


Other results indicating high geometric albedos for some hot Jupiters using Kepler:
Kepler-7b (Demory et al. 2011, ApJ, 735, 12)
HAT-7b (Christiansen et al. 2010, ApJ, 710, 97)

T. M. Evans et al. 2013, ApJL, in press (arXiv:1307.3239v1)

Cross-correlation Technique

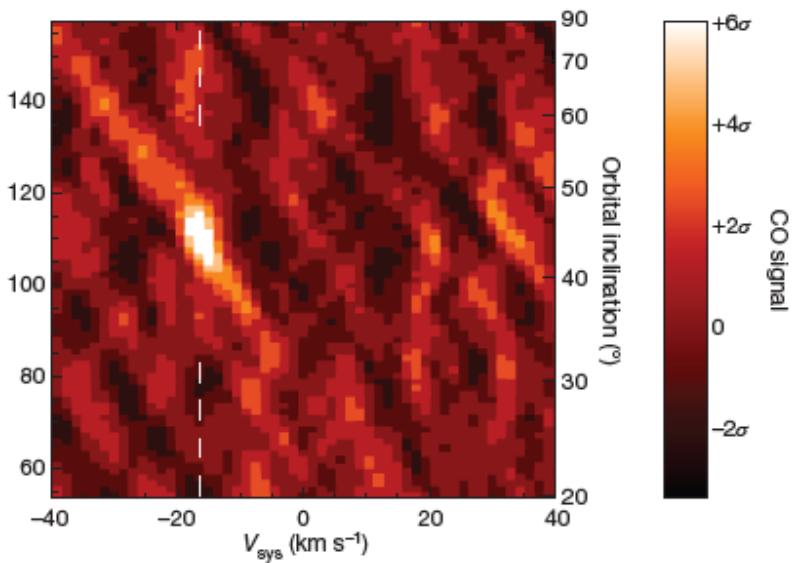
RV-Shifted Absorption from HD
209458b During Transit



Snellen et al. (2010)

CO absorption detected at 5.6σ

CO detection in the non-transiting planet τ Bootis

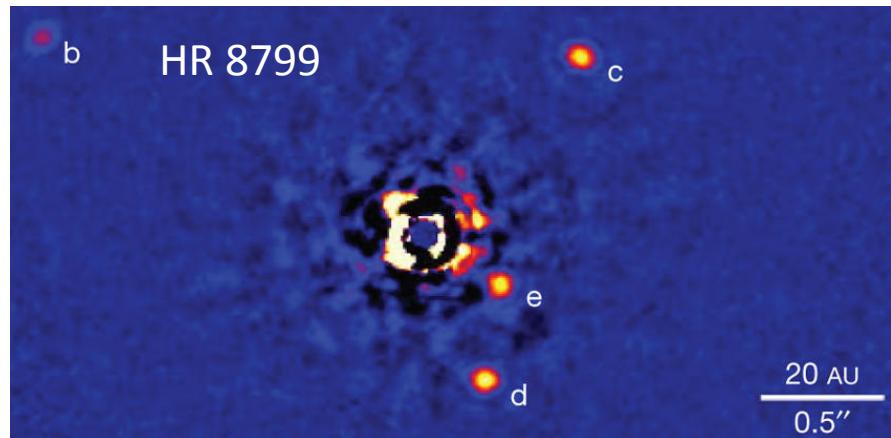


Brogi et al. (2012)
Also see Rodler et al. (2013)

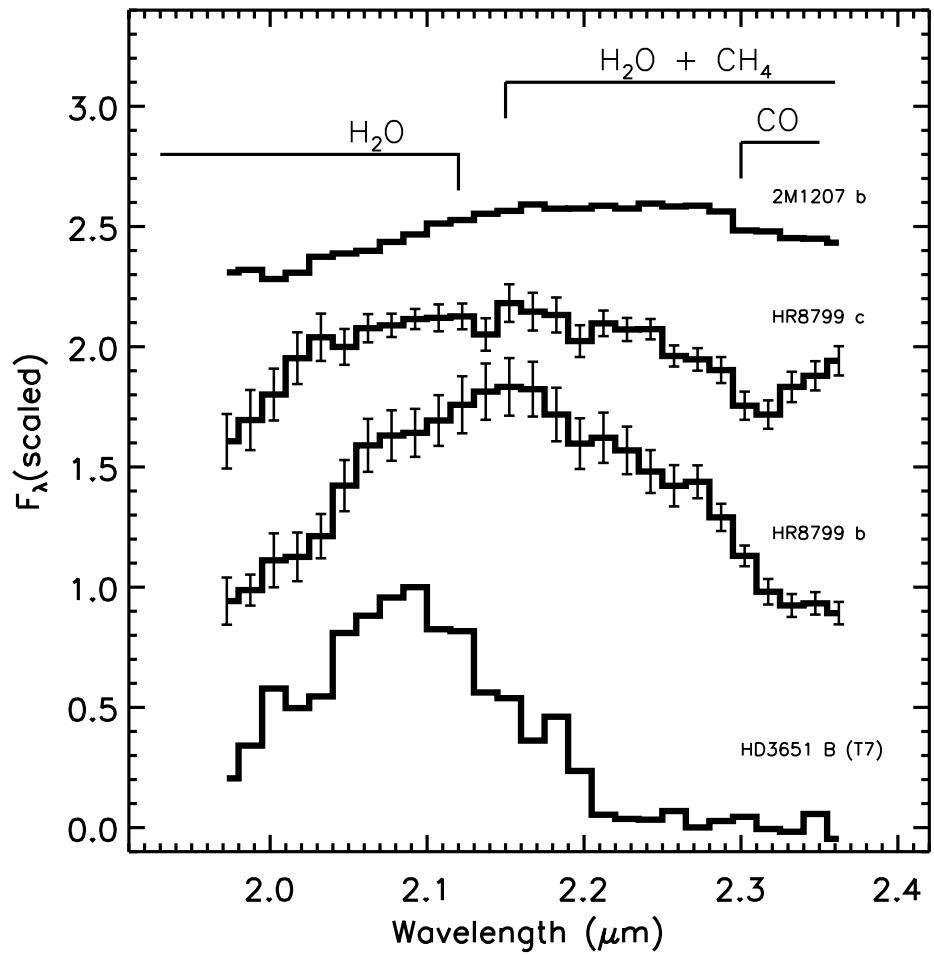
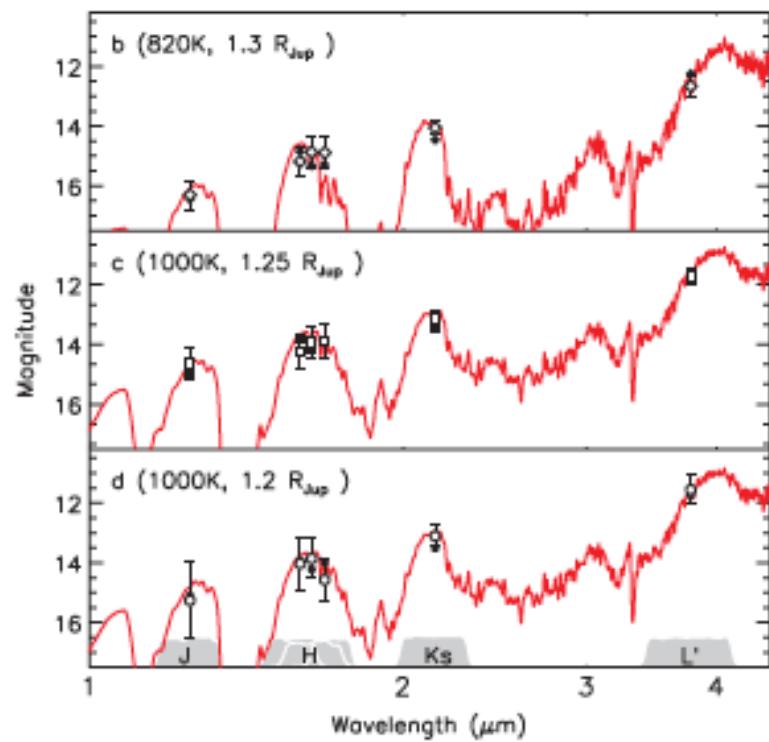
Outline

- ✧ Theory of Exoplanetary Atmospheres
- ✧ Atmospheres of Hot Jupiters
- ✧ Atmospheres of Directly-imaged Planets
- ✧ Atmospheres of Hot Neptunes
- ✧ Atmospheres of Super-Earths
- ✧ Frontier Problems and Future Outlook

Atmospheres of Directly-imaged Exoplanets

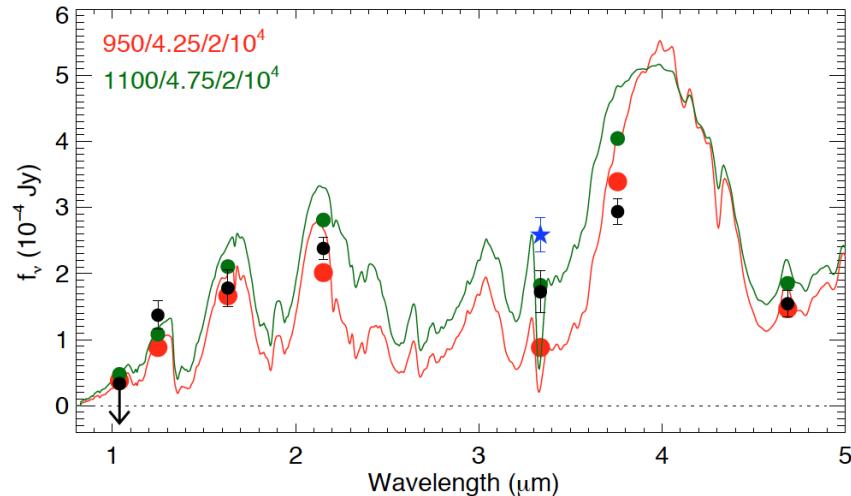


Marois et al. 2008, 2010



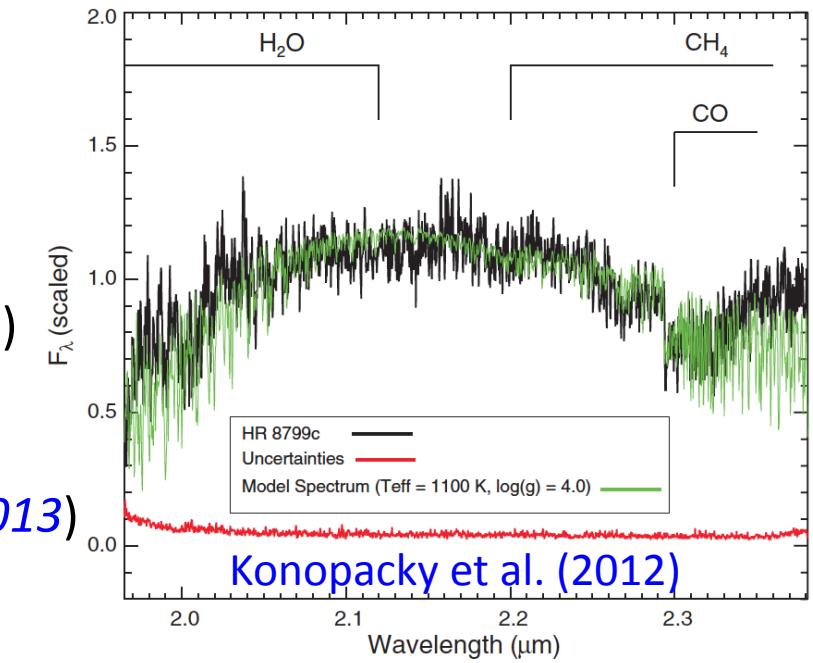
Barman et al. (2011)

Inferences for the HR 8799 system



Marley et al. (2012)

- Non-equilibrium chemistry
(Bowler et al. 2010; Barman et al. 2011)
- Thick clouds
(Barman et al. 2011; Currie et al. 2011;
Madhusudhan et al. 2011; Marley et al. 2012)
- High-resolution spectroscopy
(Janson et al. 2010; Barman et al. 2011;
Konopacky et al. 2012; Oppenheimer et al. 2013)
- Atmospheric Retrieval (Lee et al. 2013)

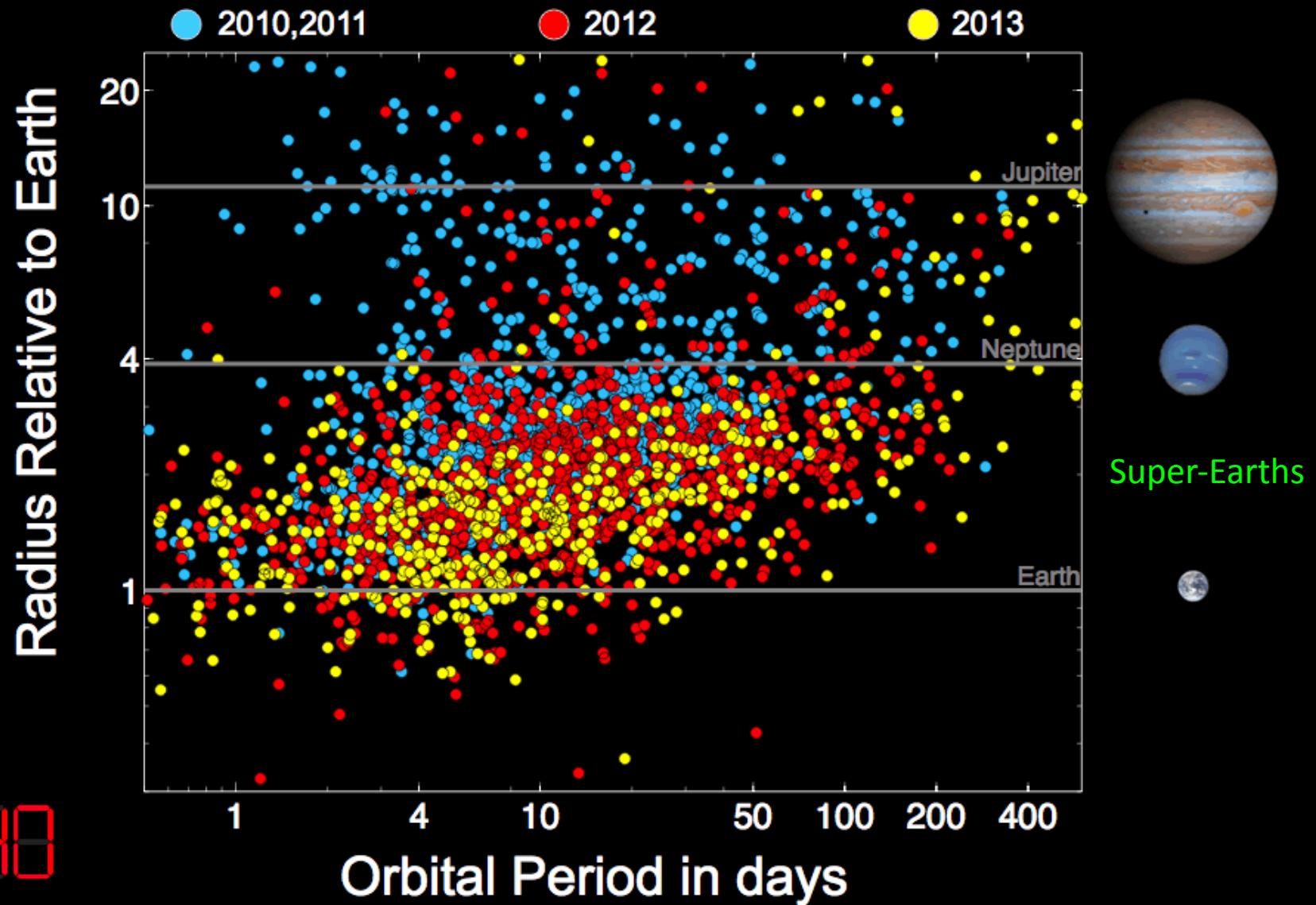


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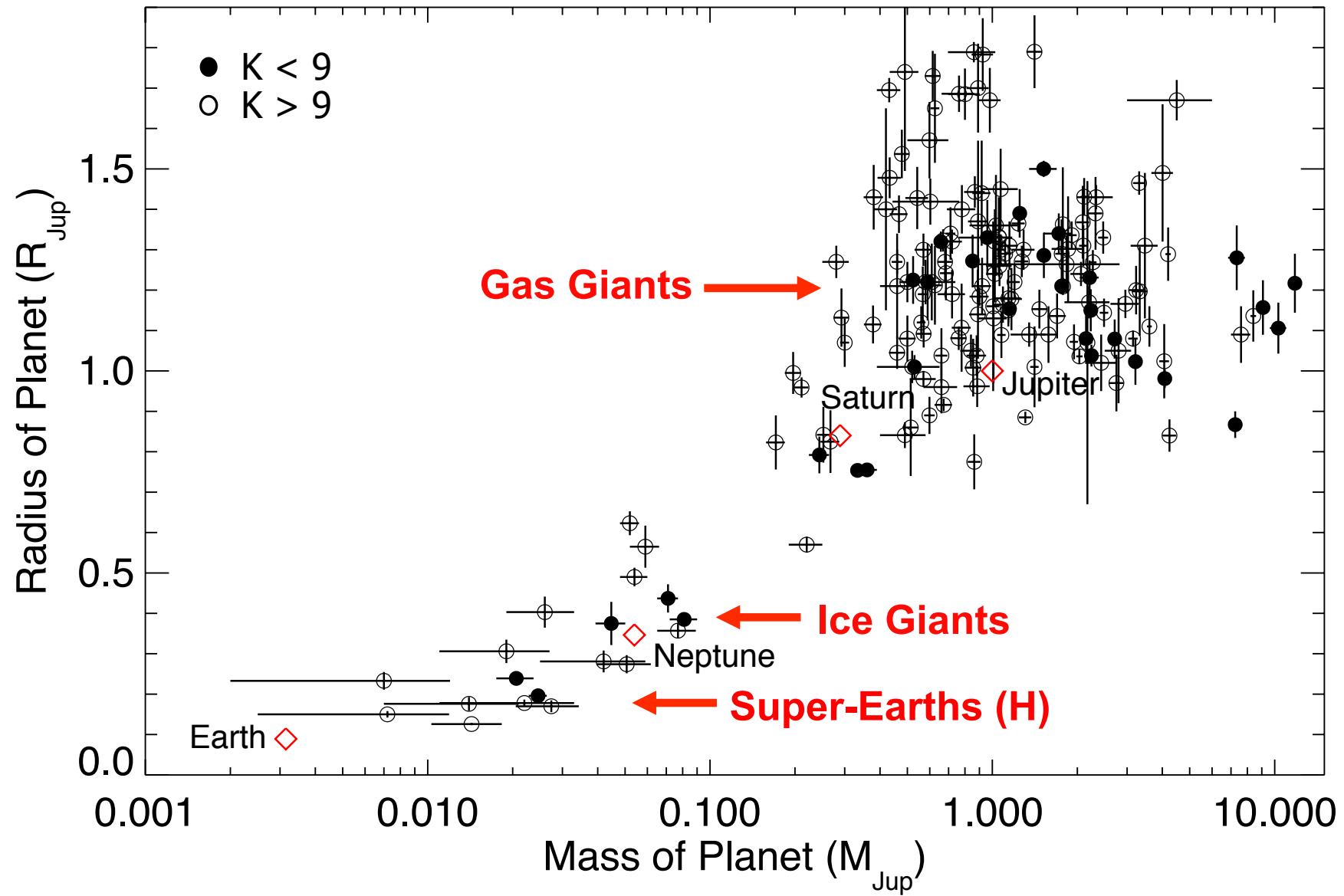
Kepler's Planet Candidates

22 Months: May 2009 - Mar 2011



2010

Prospects for Surveying Sample of Smaller Planets

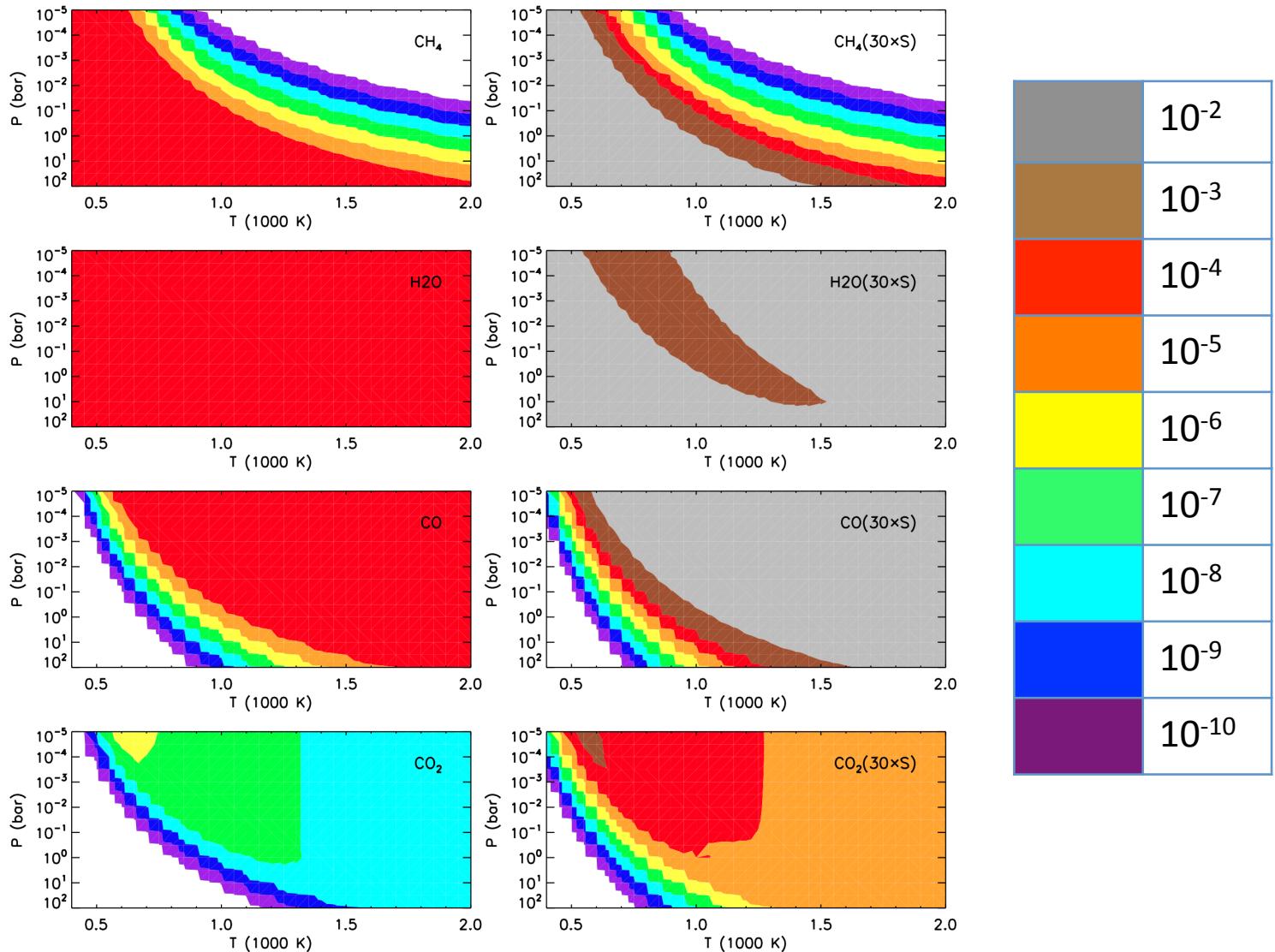


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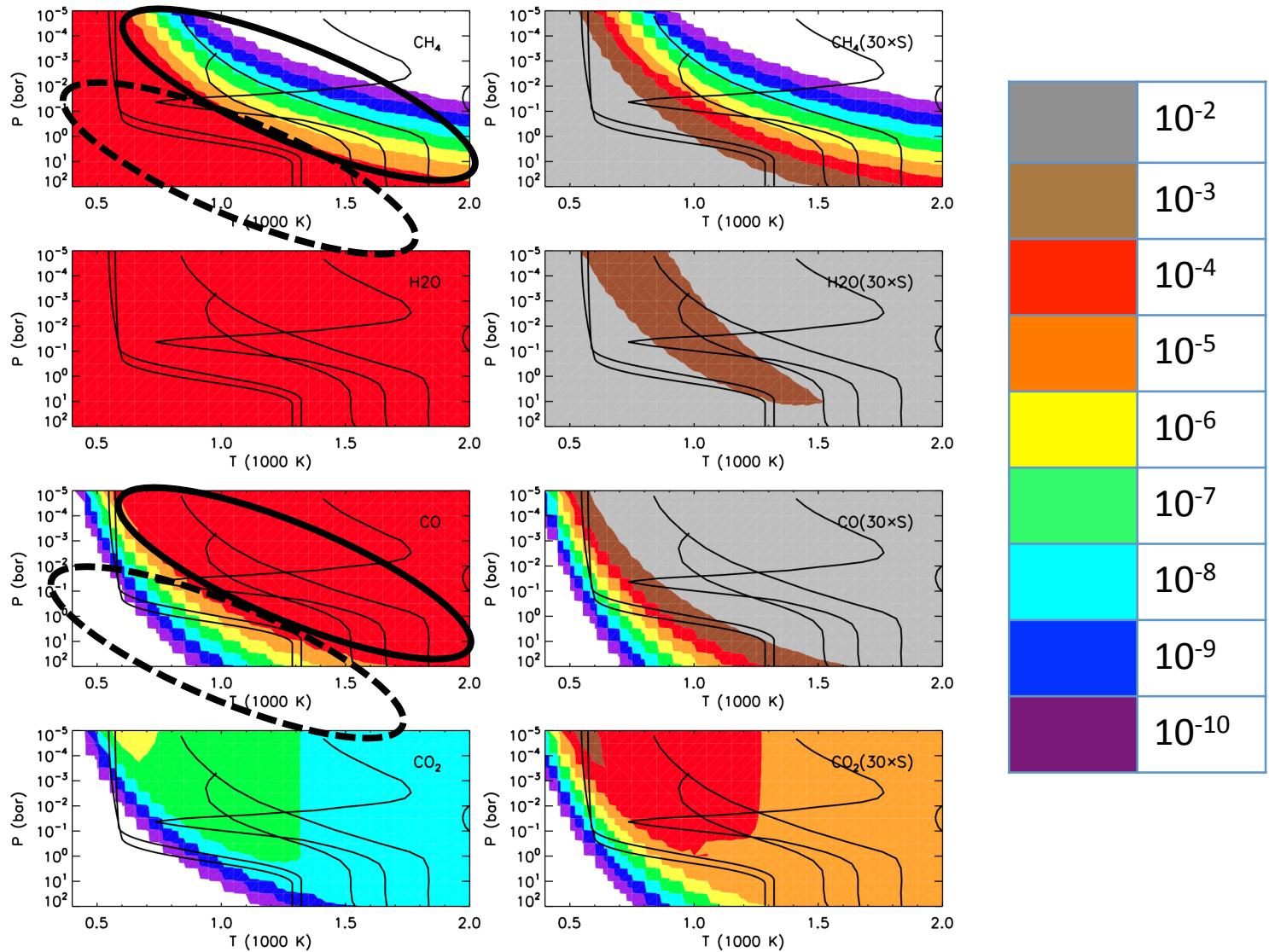
Chemistry in H₂-rich Atmospheres

(Molecular mixing ratios assuming chemical equilibrium)

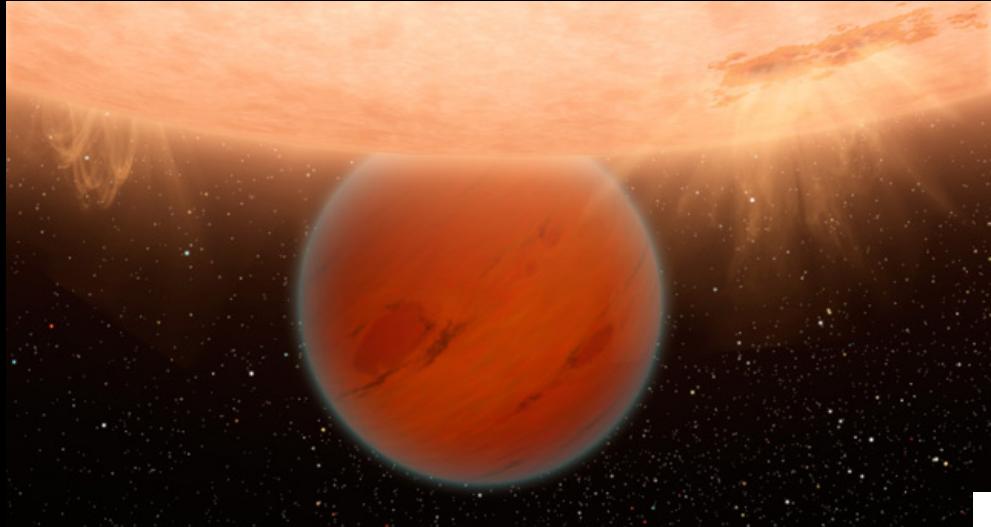


Chemistry in H₂-rich Atmospheres

(Molecular mixing ratios assuming chemical equilibrium)



The hot Neptune GJ 436b



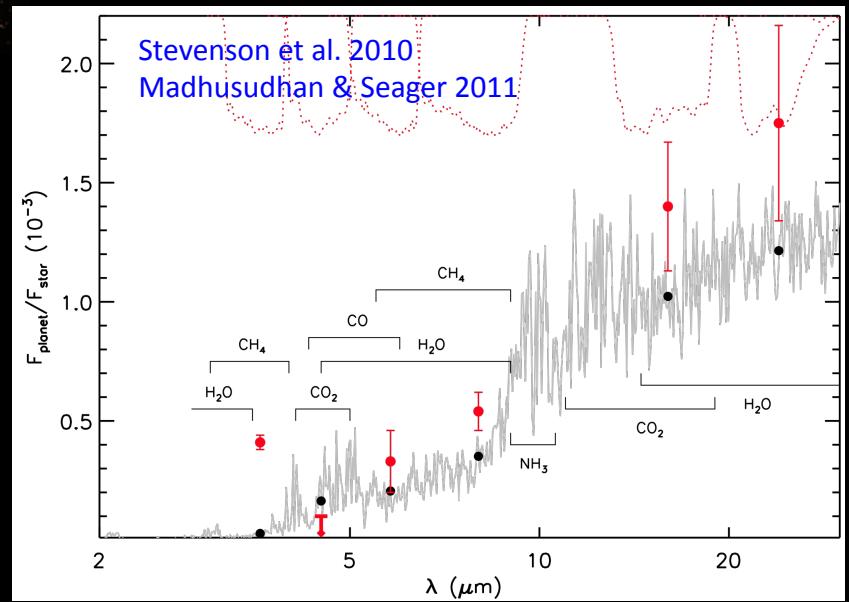
Credits: NASA/JPL-Caltech

$M_s = 0.4 M_\odot$, $R_s = 0.5 R_\odot$, $T_{\text{eff}} = 3500 \text{ K}$, M3 V

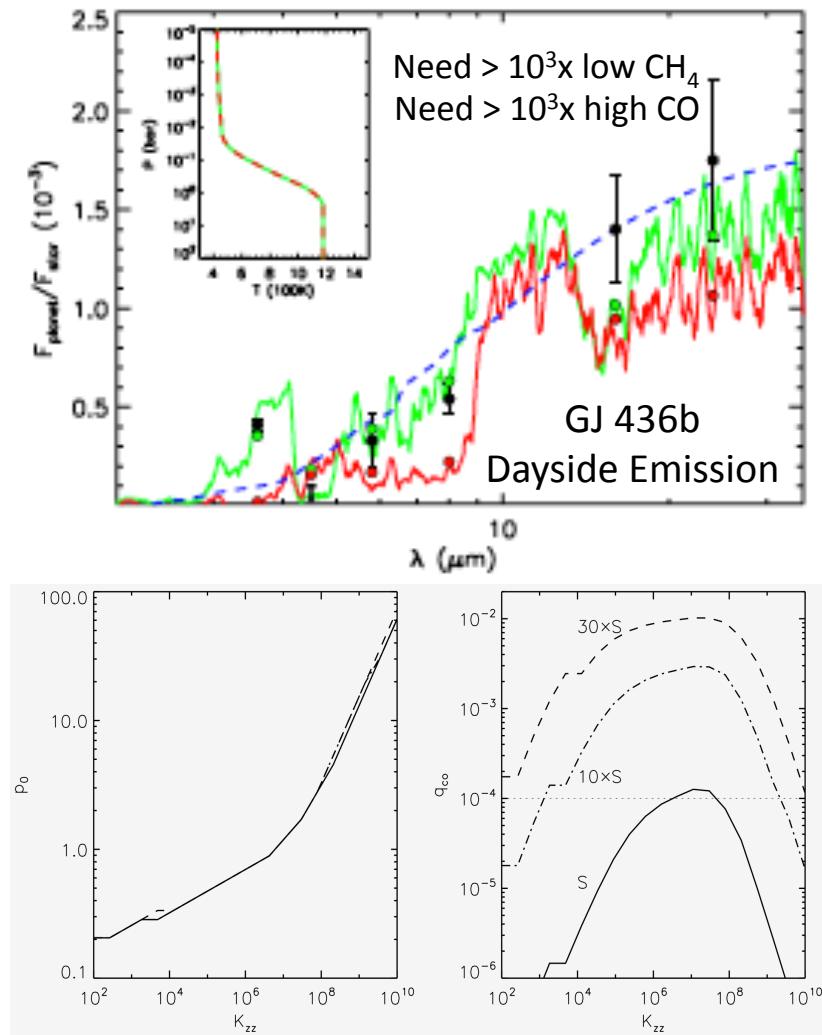
$M_p = 22.2 M_E$, $R_p = 4.3 R_E$, $T_{\text{eq}} \sim 750 \text{ K}$

$a = 0.03 \text{ AU}$, $d = 10.2 \text{ pc}$, $P = 2.6 \text{ days}$, $e = 0.15$

*Butler et al. 2004; Gillon et al. 2007;
Manness et al. 2007*



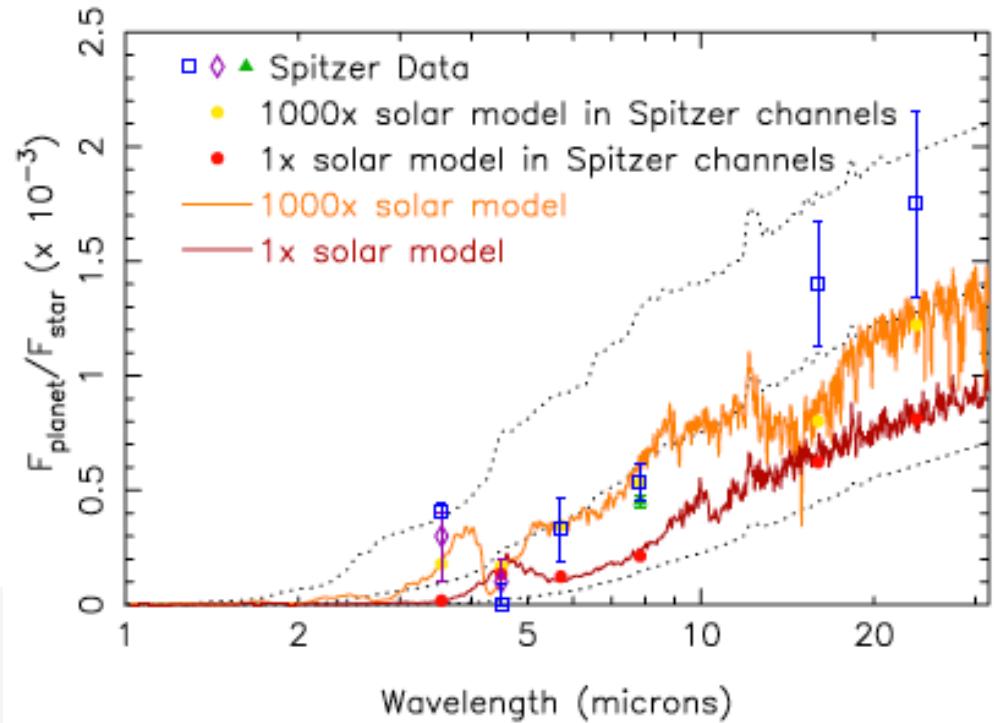
Non-Equilibrium Chemistry and High Metallicity in GJ 436b



Stevenson et al. 2010

Madhusudhan & Seager 2011

But cf Beaulieu et al. 2011; Knutson et al. 2011

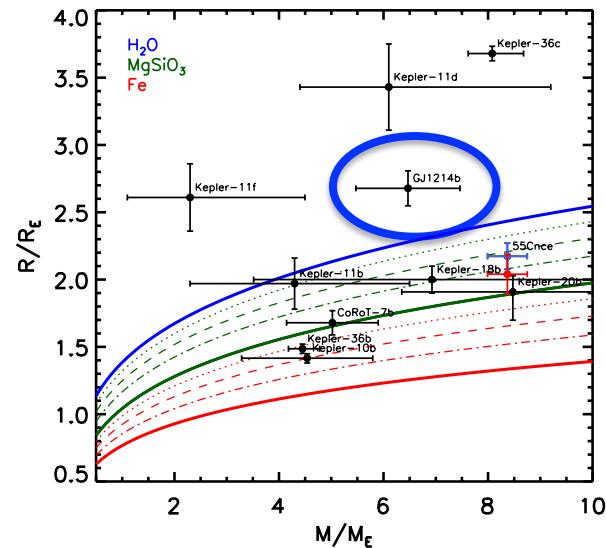


- First atmospheric detection ([Demory et al. 2009](#))
- Grid of equilibrium models ([Spiegel et al. 2010](#))
- General circulation model ([Lewis et al. 2010](#))
- Transmission Models ([Shabram et al. 2011](#))
- Non-equilibrium and very high metallicity models ([Moses et al. 2013](#))

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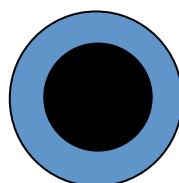
The Atmosphere of super-Earth GJ 1214b



Scale Height

$$H = \frac{kT}{g\mu}$$

H₂-rich

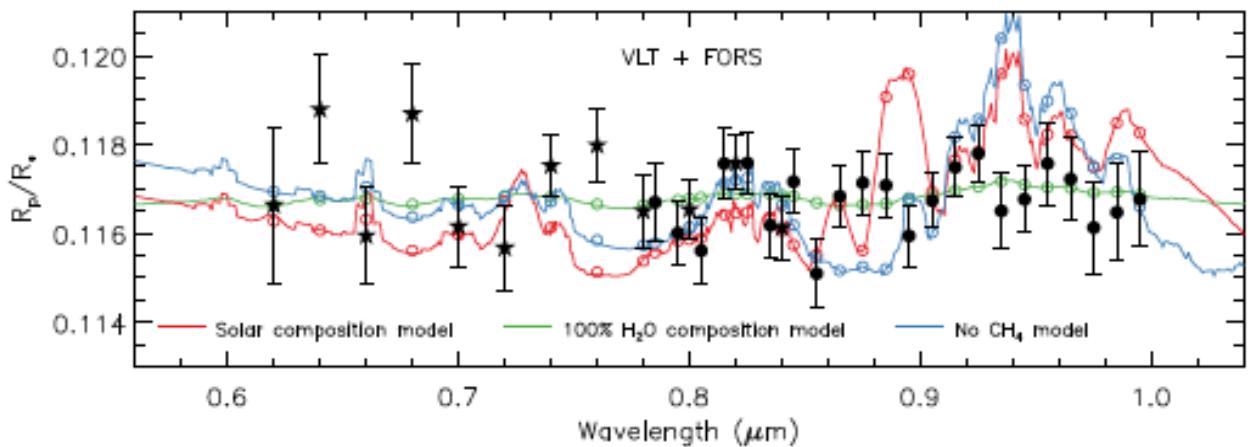
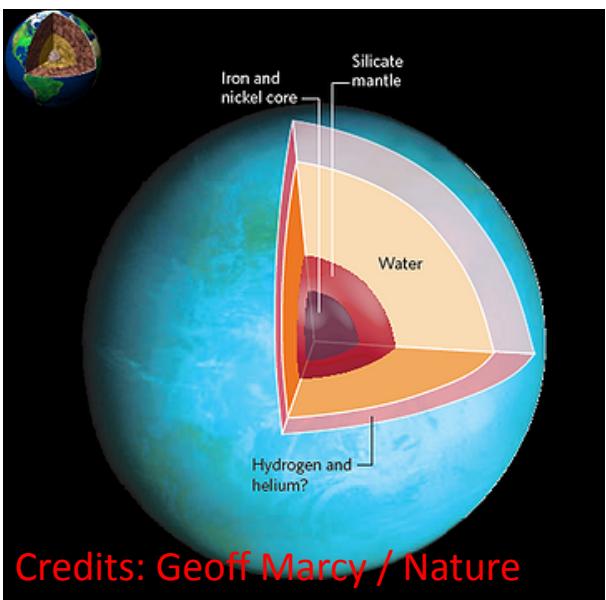


Large scale
height

H₂O-rich



Small scale
height



Bean et al. 2010, *Nature*, 468, 669;

Bean et al. 2011, *ApJ*, 743, 92

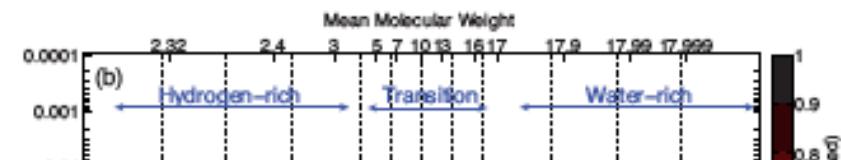
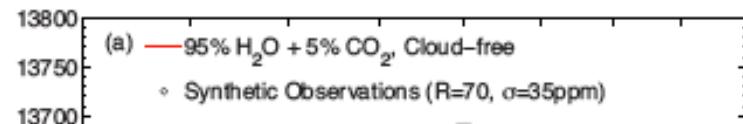
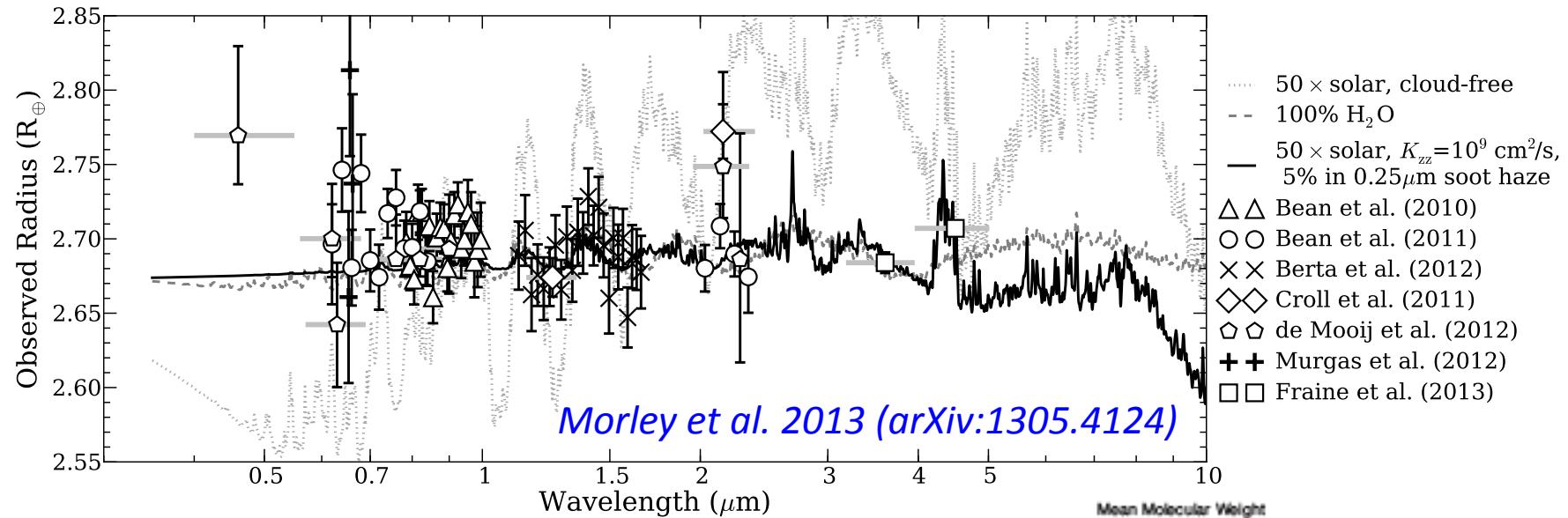
Charbonneau et al. 2009; Rogers & Seager 2009, 2010;

Miller-Ricci & Fortney 2011; Kempton et al. 2011; Desert et al. 2011;

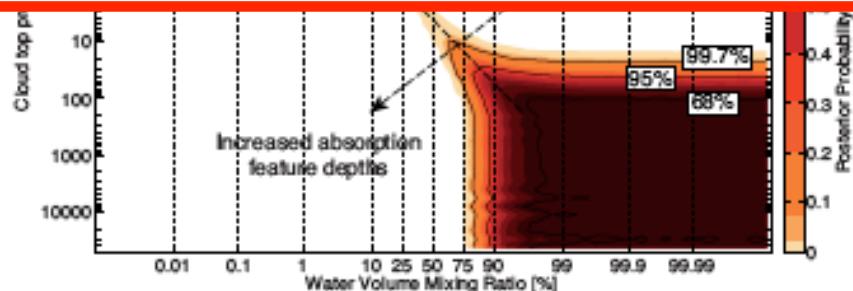
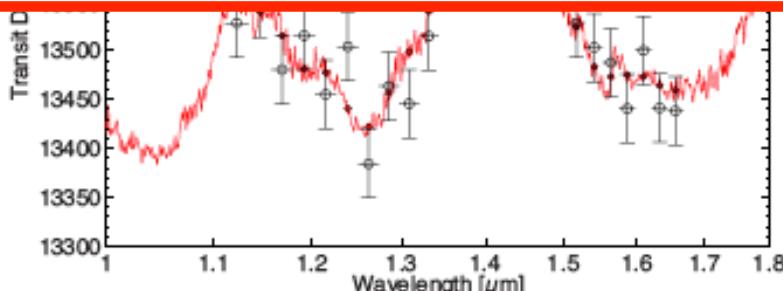
Berta et al. 2011; Croll et al. 2011; de Mooij et al. 2012; Murgas et al. 2012;

Benneke & Seager 2013; Howe & Burrows 2012; Fraine et al. 2013

Distinguishing Between Cloudy and Metal-rich Atmosphere in GJ 1214b



HST WFC3 observations with precisions better than ~ 50 ppm would be required to detect a water-rich atmosphere in GJ 1214b. This is possible by stacking up 10-15 transits.



Benneke & Seager 2013 (arXiv:1306.6325)

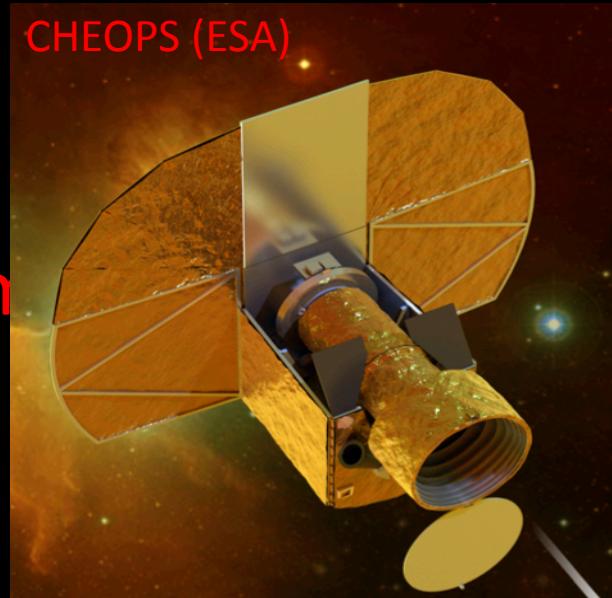
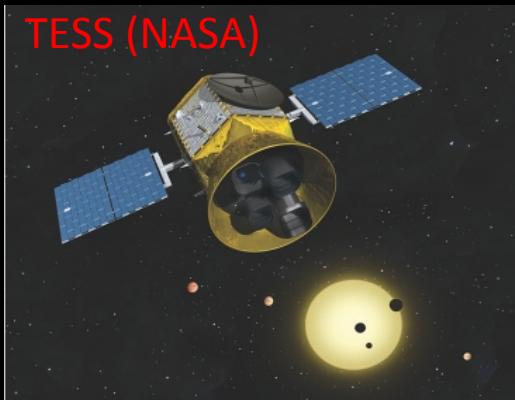
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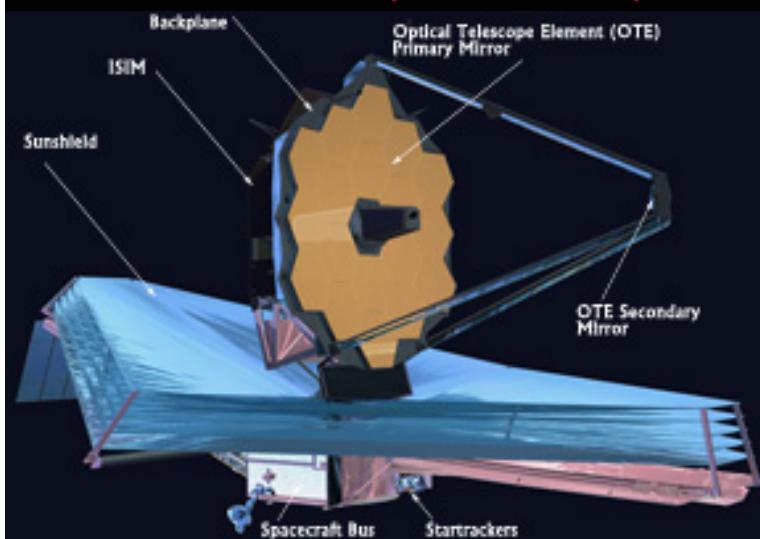
The Future of Exoplanet Science

- Detection of small planets orbiting nearby stars
- Characterization of atmospheres of exoplanets
 - To understand physical and chemical processes in exoplanetary atmospheres and interiors
 - To place constraints on planet formation and evolution

The Future of Exoplanet Science



The James Webb Space Telescope



f EChO (ESA Mission) S c The future from ground
E-ELT, GMT, TMT

