

Characterization of KOI-94 system with photometric light curves and transit timing variation analysis: implication for the planet-planet eclipse

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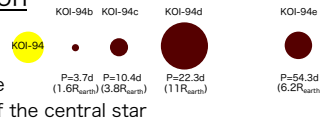
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Introduction

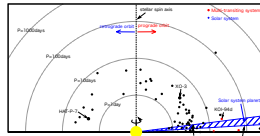
KOI-94

- Multiple-transiting planetary system discovered by the Kepler space telescope
- Four transiting planets in the proximity of the central star



Spin-orbit angle measurement

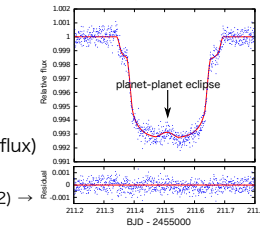
- Many hot Jupiters reside in misaligned orbits
- How about multiple-transiting systems?
- Rossiter-McLaughlin effect of KOI-94d
- **Orbital axis of KOI-94d is aligned with the stellar spin axis**



Planet-planet eclipse (PPE)

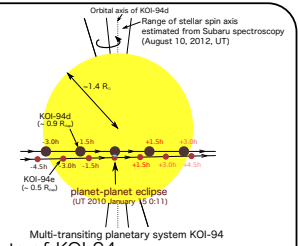
- Two planets (d and e) overlap with each other during their double-transit phase
- Shape of the "bump" (increase in the relative flux)
- **Orbital axes of KOI-94d and KOI-94e are well aligned**

Hirano et al. (2012) →



Motivation of this research

- Two close-in giant planets with well-aligned orbital axes
- quiescent disk migration?
- Important sample to understand the formation of multiple systems



Characterization of KOI-94

- Weiss et al. (2013): RV measurements of KOI-94
- Mass of KOI-94d is well constrained ($m_d = 106 \pm 11 M_J$), but the **detection of the other planets are marginal**
- Analysis of TTV can improve their estimates

Detailed study of PPE

- **Mutual inclination can be precisely constrained**
- No detailed modeling/discussion of multi-body effect

	KOI-94c	KOI-94d	KOI-94e
m (M_J)	$15.4^{+1.4}_{-1.4}$	106 ± 11	35^{+8}_{-8}
e	0.43 ± 0.23	0.022 ± 0.008	0.019 ± 0.23

Best-fit parameters by Weiss et al. (2013)

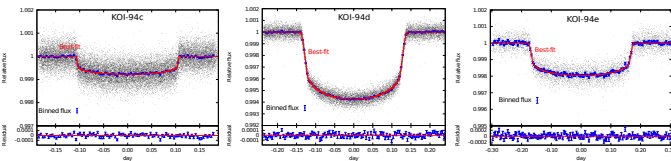
⇒ Direct N-body analysis of TTV

Evaluation of the multi-body effect on PPE

Analysis of transit light curves

Phase-folded transit light curve

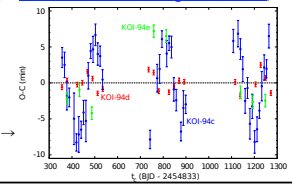
- Fix the transit parameters (a/R_s , R_p/R_s , b + limb darkening coefficients) based on the **phase-folded transit light curves**



TTV signal

- Fit for the **transit times** (t_c) of KOI-94c, KOI-94d, and KOI-94e
- Deviation from the exact periodicity (= **TTV: transit timing variation**) was extracted by the linear fit
- Amplitude, phase, shape of TTV
- **planetary mass & eccentricity**

Observed TTV signals of KOI-94c, KOI-94d, & KOI-94e



TTV analysis

Method

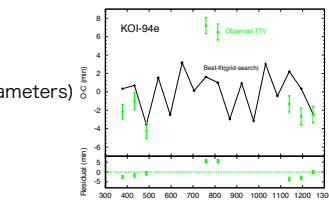
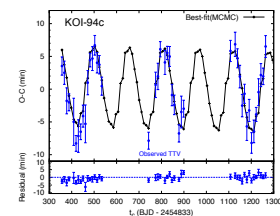
- Orbit integration using the fourth-order Hermite scheme
- positions & velocities of the planets
- Transit center = minimum of the star-planet distance
- simulated TTV → compared with the observed signal
- Fit for m (mass), e (eccentricity), ω (longitude of periastron)
- **KOI-94b was neglected** (negligible contribution to the TTVs of the other three)

Result

- **TTV of KOI-94e** → poor best-fit (not used to constrain system parameters)
- ★ **outer non-transiting planet?**

TTVs KOI-94c & KOI-94d

(fitted simultaneously)



→ Solution with relatively small masses & eccentricities

Comparison with RV result

- **Eccentricity of KOI-94c: 1.8 σ smaller than RV best-fit** ($e_c = 0.43 \pm 0.23$)
- **Mass of KOI-94d: 3-4 σ smaller**
- ★ Also supported by the analysis using the analytic TTV formula by Lithwick et al. (2012)
- Further follow-up required

Parameter	Best-fit parameters obtained from TTV analysis		
	Value ($m_d = 106M_J$)	Value ($m_d = 73M_J$)	Value (TTV only)
KOI-94c			
m_c	$11.8^{+1.6}_{-1.6}$	$13.9^{+2.7}_{-2.7}$	$9.4^{+2.4}_{-2.4}$
$e_c \cos \varpi_c$	$0.0329^{+0.0047}_{-0.0055}$	$0.0092^{+0.0264}_{-0.0059}$	$0.0143^{+0.0080}_{-0.0059}$
$e_c \sin \varpi_c$	$-0.0104^{+0.0038}_{-0.0042}$	$-0.0031^{+0.0067}_{-0.0061}$	$0.0045^{+0.0091}_{-0.0079}$
χ^2_ν	84	62	56
KOI-94d			
m_d	106 (fixed)	73 (fixed)	$52.1^{+6.9}_{-7.1}$
$e_d \cos \varpi_d$	$0.055^{+0.011}_{-0.014}$	$-0.016^{+0.064}_{-0.011}$	$-0.022^{+0.014}_{-0.011}$
$e_d \sin \varpi_d$	$0.012^{+0.011}_{-0.012}$	$0.0093^{+0.018}_{-0.018}$	$0.0075^{+0.021}_{-0.018}$
χ^2_ν	66	43	43
KOI-94e			
m_e	$15.0^{+2.4}_{-2.4}$	$12.9^{+3.0}_{-3.0}$	$13.0^{+2.5}_{-2.5}$
$e_e \cos \varpi_e$	$0.067^{+0.019}_{-0.014}$	$-0.069^{+0.018}_{-0.018}$	$-0.078^{+0.014}_{-0.014}$
$e_e \sin \varpi_e$	$0.042^{+0.017}_{-0.017}$	$-0.022^{+0.016}_{-0.016}$	$-0.023^{+0.017}_{-0.014}$
$(\chi^2_\nu + \chi^2_\alpha)/d.o.f$	150/57	110/57	99/56

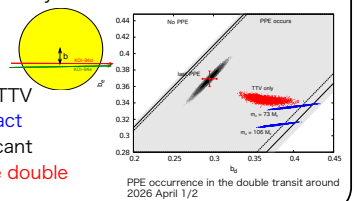
Implication for the PPE: when will it occur next?

Two-body prediction

- Occurrence of the PPE in a certain double transit
- minimum separation between planets vs. sum of planetary radii
- Analytic model neglecting the interaction among the planets
- next PPE by KOI-94d and KOI-94e occurs in the **double transit around UT 2026 April 1/2**
- What if we include the multi-body interaction?

Multi-body prediction

- Orbit integration using the parameters obtained from TTV
- Variation of the **transit impact parameter b** is most significant
- **PPE still occurs in the same double transit** (at least in 1 σ)



Summary & Outlook

- ✓ TTV analysis of KOI-94c, KOI-94d and KOI-94e
- Mass, eccentricity, longitude of periastron
- Solution with small eccentricities & small m_j
- ✓ Multi-body effect is not significant for the time of the next PPE
- Discrepancy between TTV and RV results
- Four-planet model may not fully describe the system
- TTV of KOI-94e cannot be explained (another perturber?)
- Direct fit to the transit times (not TTVs) are not successful (?)
- Interesting target of further study

References

- Hirano, T., et al. 2012, ApJ, 759, L36
- Weiss, L. M., et al. 2013, ApJ, 768, 14
- Lithwick, Y., Xie, J., & Wu, Y. 2012, ApJ, 761, 122